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by

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## Abstract

We explore the macroeconomic effects of a compression in the long-term bond yield spread within the context of the Great Recession of 2007-2009 via a time-varying parameter structural VAR model. We identify a ‘pure’ spread shock defined as a shock that leaves the policy rate unchanged, which allows us to characterize the macroeconomic consequences of a decline in the yield spread induced by central banks’ asset purchases within an environment in which the policy rate is constrained by the effective zero lower bound. Two key findings stand out. First, compressions in the long-term yield spread exert a powerful effect on both output growth and inflation. Second, conditional on available estimates of the impact of the Federal Reserve’s and the Bank of England’s asset purchase programs on long-term yield spreads, our counterfactual simulations suggest that U.S. and U.K. unconventional monetary policy actions have averted significant risks both of deflation and of output collapses comparable to those that took place during the Great Depression.

*JEL classification: C11, C32, E52, E58*

*Bank classification: Monetary policy framework; Interest rates; Econometric and statistical methods; Transmission of monetary policy*

## Résumé

Les auteurs étudient les effets macroéconomiques d’un rétrécissement des écarts entre les rendements obligataires à long terme pendant la Grande Récession de 2007-2009 à l’aide d’un modèle VAR structurel à paramètres variables dans le temps. Ils identifient un choc « pur » sur les écarts, c.-à-d. un choc qui laisse le taux directeur inchangé. Cette démarche leur permet de décrire les conséquences macroéconomiques d’une réduction des écarts de rendement induite par les achats d’actifs qu’effectuent les banques centrales au sein d’un environnement où le taux directeur est soumis à la contrainte d’un niveau plancher. L’étude aboutit à deux constats. D’un côté, la réduction des écarts à long terme exerce une influence considérable sur la croissance de la production tout comme sur l’inflation. De l’autre, sur la base des estimations disponibles concernant l’effet qu’ont eu les programmes d’achat d’actifs mis en œuvre par la Réserve fédérale américaine et la Banque d’Angleterre sur les écarts de rendement à long terme, les résultats des simulations contrefactuelles semblent indiquer que les mesures de politique monétaire non traditionnelles déployées aux États-Unis et au Royaume-Uni ont permis d’éviter la matérialisation de risques importants, à savoir une déflation et un effondrement de la production aussi graves qu’à l’époque de la Grande Crise.

*Classification JEL : C11, C32, E52, E58*

*Classification de la Banque : Cadre de la politique monétaire; Taux d’intérêt; Méthodes économétriques et statistiques; Transmission de la politique monétaire*

The decisive policy easing by the Fed and the ECB during the crisis, and the adoption of unconventional measures by the two central banks, was crucial in countering the threat of deflation in the current episode.

—Athanasios Orphanides<sup>1</sup>

## 1 Introduction

In response to the 2007-2009 financial crisis, all major central banks aggressively lowered their policy rate. Once the effective zero lower bound on the short-term nominal interest rate was reached, policymakers resorted to unconventional tools to provide further stimulus in light of the significant deterioration of economic conditions and the risks of deflation. Among these non-standard monetary policy operations, the large-scale asset purchases conducted by the Federal Reserve and the Bank of England from early 2009 onwards attracted considerable attention. These operations entailed withdrawing large quantities of longer-term Treasury securities from the private sector through purchases in the secondary market, thereby changing the relative supplies of short-term and long-term bonds and other assets available to the public. The primary objective of these quantitative easing policies was to put downward pressure on long-term interest rates in order to support private borrowing of households and businesses, thus spurring aggregate demand and real economic activity. This paper addresses two questions. First, we investigate how effective central banks' unconventional monetary policy actions were in countering the recessionary shocks associated with the 2007-2009 financial crisis. The underlying thought experiment is a counterfactual simulation of how output, inflation and unemployment would have evolved, had the asset purchase programs never existed. Second, we evaluate more generally how powerful central bank interventions are at the zero lower bound, when the traditional instruments for conducting monetary policy are no longer available.

In order to quantify the macroeconomic implications of these policies, it is necessary to establish first how effective large-scale asset purchases are at compressing the government bond yield spread once the zero lower bound becomes binding. The latter question has been addressed by a number of recent papers, including Gagnon, Raskin, Remache, and Sack (2011), D'Amico and King (2010), Hamilton and Wu (2012), Krishnamurthy and Vissing-Jorgensen (2011) and Doh (2010) for the U.S., and Meier (2009) and Joyce, Lasiosa, Stevens, and Tong (2011) for the U.K. These studies employ a variety of time-series and event-study approaches and all reach the conclusion that the asset purchase programs were successful at flattening the yield curve. In fact, they find a substantial reduction in longer-term yields as a result of quantitative easing measures.

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<sup>1</sup>Keynote Speech by Athanasios Orphanides, Governor, Central Bank of Cyprus, at the 'International Research Forum on Monetary Policy', Federal Reserve Board, March 27, 2010.

Assessing the financial market effects of asset purchases is only a first step in gauging the effectiveness of unconventional monetary policy actions, however, because the ultimate goal of the central bank is to counteract deflationary pressures and to foster economic growth and employment. Our paper focuses on this latter question. Specifically, we take the estimates of the effects of bond purchases on the spread as given and ask what the macroeconomic consequences of a compression in the yield spread are when short-term interest rates are constrained by the zero lower bound.

Chung, Laforte, Reifschneider, and Williams (2012) recently have addressed this question within the Federal Reserve Board’s large-scale macroeconomic model. Their counterfactual simulations indicate that the expansion of the Federal Reserve’s balance sheet has kept the unemployment rate from rising to levels that would have prevailed in the absence of asset purchases and has likely averted a deflationary spiral for the U.S. economy. Similar conclusions are reached by Del Negro, Eggertsson, Ferrero, and Kiyotaki (2010) and Chen, Cúrdia, and Ferrero (2011) based on medium-sized DSGE models with an explicit role for the zero bound on nominal interest rates. Lenza, Pill, and Reichlin (2010) also assess the macroeconomic effects of a decline in interest rate spreads for a given level of the policy rate for the Euro area. They focus on the likely impact of the ECB’s non-standard policy actions on the short-end of the yield curve by contrasting macroeconomic outcomes resulting from a policy versus a no-policy scenario which differ only in the evolution of short-term interest rates. Put differently, in order to gauge the effectiveness of policy intervention in warding off disastrous macroeconomic consequences, they conduct a forecasting exercise of key variables conditional upon a counterfactual path and an observed path of money market rates based on a reduced-form large Bayesian VAR model estimated over the pre-crisis period. While they show that the narrowing of spreads induces economic stimulus, these beneficial effects take hold only with a considerable delay.

A common feature of all these analyses is that they build on the premise that the historically observed relationships uncovered in the data have not been affected by the most recent episode of financial turmoil. There is reason to doubt that the underlying behavioral relationships have remained unaltered given the severe economic dislocations in the aftermath of the financial crisis. We instead propose to explore the macroeconomic effects of a compression in the long-term bond yield spread within the context of the Great Recession of 2007-2009 by estimating a time-varying parameter structural VAR (TVP-VAR) model for the U.S. and the U.K. economies. Within this framework, we define a ‘pure’ spread shock as a disturbance that leaves the short-term policy rate unchanged, which allows us to characterize the responses of macroeconomic aggregates to a decline in long-term yield spreads induced by central banks’ bond purchase programs under circumstances where the short rate cannot move, which is exactly the situation encountered at the zero lower bound. This shock is identified by means of a combination of sign restrictions and a *single* zero restriction.

Our empirical analysis yields several intriguing results. First, we show that a compression in the long-term yield spread exerts a powerful positive effect on both output growth and

inflation when monetary policy is constrained by the effective zero lower bound. Second, our evidence clearly highlights the importance of allowing for time variation in the transmission of a spread compression to the macroeconomy. For example, the effect on U.S. inflation was particularly large during the Great Inflation of the 1970s, the recession of the early 1990s, and the most recent past, whereas the 1990s were characterized by significantly weaker responses. By the same token, in the U.K. the impact on both inflation and output growth appears to have become stronger in recent years. This implies, for the present purposes, that the use of fixed-coefficient models estimated over (say) the last two decades would underestimate the impact resulting from yield spread compressions engineered by central banks *via* asset purchase programs in offsetting the adverse shocks associated with the 2007-2009 financial crisis. Third, conditional on Gagnon *et al.*'s (2011) estimates of the impact of the Federal Reserve's bond purchases on the 10-year government bond yield spread, our counterfactual simulations indicate that U.S. unconventional monetary policy actions have averted significant risks both of deflation and of severe output collapses comparable to those that took place during the Great Depression. We show that without the large-scale asset purchase program the U.S. economy would have been in deflation for two quarters with annualized inflation being as low as minus one percent in 2009Q2, annualized real GDP growth would have contracted by 10% in the first quarter of 2009, and the unemployment rate would have been consistently above its actual value throughout 2009 reaching 10.6% at the end of 2009. A similar picture emerges for the U.K. conditional on Charlie Bean's (2009) broad estimate of the impact of the Bank of England's gilt purchases on long-term yield spreads without which inflation would have fallen to minus 4 percent and output growth would have dropped by 12 percent at annual rates.

The remainder of the paper is structured as follows. The next section outlines the key features of the time-varying parameter VAR model, discusses the reasons behind such a modelling choice, and describes the identification strategy and the motivation behind it. Section 3 presents the empirical evidence. Section 4 concludes.

## 2 Empirical methodology

The use of a time-varying parameter specification is of particular importance in the present context since it allows us to capture the macroeconomic structure in place during the Great Recession of 2007-2009 when tracing the effects of a compression in the bond yield spread induced by central bank's unconventional monetary policies. In this respect, the use of fixed-coefficient models would be unadvisable for at least two reasons. First, the notion that key structural macroeconomic relationships have remained unchanged in face of the dramatic economic contraction associated with the financial crisis is entirely open to question. Second, at a very general level, there is widespread evidence of instabilities in macroeconomic time series (see, e.g., Stock and Watson 1996) and of changing volatility in the U.S. and the

U.K. economies (see, e.g., McConnell and Pérez-Quirós 2000; Benati 2008). In fact, previous empirical studies of the transmission of *conventional* monetary policy provide evidence in support of models that feature smoothly evolving coefficients and heteroskedastic shocks (e.g., Primiceri 2005; Canova and Gambetti 2009; Koop, Leon-Gonzalez, and Strachan 2009; Baumeister, Liu, and Mumtaz 2011).

While many models may potentially be able to account for some time variation in the parameters, a TVP-VAR structure is the most flexible and encompassing model specification since it does not impose strong restrictions on the evolution of the economic relationships. Although many periods over the sample are likely to be characterized by slow-moving but continuous structural changes, it cannot be excluded that the financial crisis led to a rupture in the economic structure due to its severity. However, as noted by Benati and Mumtaz (2007) and more formally demonstrated by Baumeister and Peersman (2012) by means of a Monte Carlo study, drifting coefficient models in practice are able to capture such discrete breaks if they occur.

## 2.1 A time-varying parameter VAR with stochastic volatility

We model the joint behavior of the short-term nominal interest rate, the spread between the 10-year Treasury bond yield and the policy rate, GDP deflator inflation, and real GDP growth as a VAR( $p$ ) model with time-varying parameters and stochastic volatility as in Cogley and Sargent (2005), Primiceri (2005), and Cogley, Primiceri, and Sargent (2010):

$$Y_t = B_{0,t} + B_{1,t}Y_{t-1} + \dots + B_{p,t}Y_{t-p} + u_t \equiv X_t'\theta_t + u_t \quad (1)$$

where  $Y_t \equiv [r_t, s_t, \pi_t, y_t]'$  is a  $N \times 1$  vector of endogenous variables.<sup>2</sup> The time-varying intercepts  $B_{0,t}$  and the matrices of time-varying coefficients  $B_{1,t \dots p,t}$  are collected in the vector  $\theta_t$ , and  $X_t$  is a matrix including lags of  $Y_t$  and a constant to obtain the state-space representation of the model. The  $u_t$  in the observation equation is a  $N \times 1$  vector of unconditionally heteroskedastic disturbance terms. The data frequency is quarterly. Consistent with the vast majority of papers in the literature, and for reasons of computational feasibility, the lag order is set to  $p = 2$ . Following, e.g., Cogley and Sargent (2002, 2005), and Primiceri (2005), the VAR's time-varying parameters  $\theta_t$  are postulated to evolve according to

$$p(\theta_t \mid \theta_{t-1}, Q_t) = I(\theta_t) f(\theta_t \mid \theta_{t-1}, Q_t) \quad (2)$$

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<sup>2</sup>The GDP deflator and real GDP were transformed to annualized quarter-on-quarter rates of growth, while the short-term rate and the yield spread are included in levels. For a description of the data sources for the U.S. and the U.K., see Appendix A.

with  $I(\theta_t)$  being an indicator function that rejects unstable draws, thereby enforcing a stationarity constraint on the VAR,<sup>3</sup> and with  $f(\theta_t | \theta_{t-1}, Q_t)$  given by

$$\theta_t = \theta_{t-1} + \eta_t \quad (3)$$

with  $\eta_t \equiv [\eta_{1,t}, \eta_{2,t}, \dots, \eta_{N \cdot (1+Np),t}]'$  where  $\eta_t \sim N(0, Q_t)$ . In the spirit of Cogley, Primiceri, and Sargent (2010), we introduce a stochastic volatility specification for the evolution of the covariance matrix of the innovations in the law of motion of the VAR coefficients,  $Q_t$ . Specifically, we assume that  $Q_t$  is given by

$$Q_t \equiv \begin{bmatrix} q_{1,t} & 0 & \dots & 0 \\ 0 & q_{2,t} & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & q_{N \cdot (1+Np),t} \end{bmatrix} \quad (4)$$

with the  $q_{i,t}$ 's,  $i = 1, \dots, N \cdot (1 + Np)$ , evolving as geometric random walks:  $\ln q_{i,t} = \ln q_{i,t-1} + \omega_{i,t}$ . This specification allows for a time-varying drift which is a desirable feature since key macroeconomic variables have been remarkably volatile during the Great Inflation of the 1970s, extremely stable during the Great Moderation period, and, in the case of output growth and interest rates, once again very volatile during the Great Recession. The traditional, 'first-generation' time-varying parameter models (see, e.g., Cogley and Sargent 2005; Primiceri 2005) have a hard time fitting such a pattern of time variation successfully, as they postulate that the extent of random-walk drift is constant over the sample. As a result, they tend to 'under-drift' (that is, to drift too little) during the Great Inflation, and to 'over-drift' (that is, to drift too much) during the Great Moderation, thus automatically distorting inference. Instead, a model that features a *time-specific* extent of random-walk time variation in the VAR's coefficients is more appropriate to capture such changes over time in the macroeconomic structure. Specifically, it allows the dynamics of the time-varying coefficients 'to lay dormant' in stable periods and to pick up speed in volatile periods in a data-driven way, depending on the information contained in the sample.<sup>4</sup>

The VAR's reduced-form innovations in (1) are postulated to be zero-mean normally distributed with time-varying covariance matrix  $\text{Var}(u_t) \equiv \Omega_t$  which, following established practice, we factor as:

$$\Omega_t = A_t^{-1} H_t (A_t^{-1})' . \quad (5)$$

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<sup>3</sup>It is important to be clear about the meaning of such a stationarity constraint. Although inflation contains a stochastic trend due to the time-varying parameter specification (1), the constraint (2) implies that its fluctuations *around* such a trend cannot be explosive.

<sup>4</sup>Note that this specification is somewhat simpler than the one suggested by Cogley, Primiceri, and Sargent (2010), who factor the covariance matrix of the innovations to the state equation for the time-varying parameters as  $Q_t = (B_s^{-1})' H_{s,t} B_s^{-1}$ , where  $H_{s,t}$  has exactly the same specification which we postulated for  $Q_t$ , and  $B_s$  is a lower triangular matrix with ones along the main diagonal and static covariance parameters. Thus, our specification is obtained from Cogley *et al.*'s by setting  $B_s$  equal to the identity matrix. Figures 3A and 4A in the appendix show that our model accurately tracks the trends in inflation and output growth for the U.S. and the U.K. suggesting that this specification works well in our setting.

$H_t$  is a diagonal matrix that contains the stochastic volatilities that capture changes in the magnitude of structural shocks, and  $A_t$  is a lower triangular matrix that models the contemporaneous interactions among the endogenous variables, which are defined as:

$$H_t \equiv \begin{bmatrix} h_{1,t} & 0 & 0 & 0 \\ 0 & h_{2,t} & 0 & 0 \\ 0 & 0 & h_{3,t} & 0 \\ 0 & 0 & 0 & h_{4,t} \end{bmatrix} \quad A_t \equiv \begin{bmatrix} 1 & 0 & 0 & 0 \\ \alpha_{21,t} & 1 & 0 & 0 \\ \alpha_{31,t} & \alpha_{32,t} & 1 & 0 \\ \alpha_{41,t} & \alpha_{42,t} & \alpha_{43,t} & 1 \end{bmatrix} \quad (6)$$

with the  $h_{i,t}$ 's evolving as geometric random walks,

$$\ln h_{i,t} = \ln h_{i,t-1} + \nu_{i,t} . \quad (7)$$

As in Primiceri (2005), we postulate that the non-zero and non-unity elements of the matrix  $A_t$ —which we collect in the vector  $\alpha_t \equiv [\alpha_{21,t}, \dots, \alpha_{43,t}]'$ —evolve as driftless random walks,

$$\alpha_t = \alpha_{t-1} + \tau_t \quad (8)$$

and we assume the vector  $[\epsilon'_t, \tau'_t, \nu'_t, \omega'_t]'$ , with  $\epsilon_t$  derived from the relationship  $u_t \equiv A_t^{-1} H_t^{\frac{1}{2}} \epsilon_t$ , to be distributed as  $N(0, V)$ , with

$$V = \begin{bmatrix} I_4 & 0 & 0 & 0 \\ 0 & S & 0 & 0 \\ 0 & 0 & Z_\nu & 0 \\ 0 & 0 & 0 & Z_\omega \end{bmatrix}, \quad Z_\nu = \begin{bmatrix} \sigma_{\nu,1}^2 & 0 & 0 & 0 \\ 0 & \sigma_{\nu,2}^2 & 0 & 0 \\ 0 & 0 & \sigma_{\nu,3}^2 & 0 \\ 0 & 0 & 0 & \sigma_{\nu,4}^2 \end{bmatrix} \quad \text{and} \quad (9)$$

$$Z_\omega = \begin{bmatrix} \sigma_{\omega,1}^2 & 0 & \dots & 0 \\ 0 & \sigma_{\omega,2}^2 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & \sigma_{\omega, N \cdot (1+Np)}^2 \end{bmatrix}$$

Finally, following Primiceri (2005), we adopt the additional simplifying assumption of a block-diagonal structure for  $S$  of the following form:

$$S \equiv \text{Var}(\tau_t) = \begin{bmatrix} S_1 & 0_{1 \times 2} & 0_{1 \times 3} \\ 0_{2 \times 1} & S_2 & 0_{1 \times 3} \\ 0_{3 \times 1} & 0_{3 \times 2} & S_3 \end{bmatrix} \quad (10)$$

with  $S_1 \equiv \text{Var}(\tau_{21,t})$ ,  $S_2 \equiv \text{Var}([\tau_{31,t}, \tau_{32,t}]')$ , and  $S_3 \equiv \text{Var}([\tau_{41,t}, \tau_{42,t}, \tau_{43,t}]')$ , which implies that the non-zero and non-unity elements of  $A_t$  belonging to different rows evolve independently. As discussed in Primiceri (2005, Appendix A.2), this assumption drastically simplifies inference and increases the efficiency of the estimation algorithm in an already highly-parameterized model since it allows to do Gibbs sampling on the non-zero and non-unity elements of  $A_t$  equation by equation.

We estimate (1)-(10) *via* standard Bayesian methods described in Kim and Nelson (1999). Appendix B discusses our choices for the priors, describes the Markov Chain Monte Carlo algorithm we use to simulate the joint posterior distribution of the hyperparameters and the states conditional on the data, and provides evidence of convergence to the ergodic distribution.

## 2.2 Identification of a ‘pure’ spread shock

A key insight that motivated the unconventional policy interventions in the Treasury market was that a narrowing of the long-short spread of government bonds spurs real economic activity and stems the decline in inflation by removing duration risk from portfolios of market participants and by reducing the borrowing costs for the private sector (see Bernanke 2006, 2010). Empirical evidence for a negative relationship between the term premium and future real economic activity has been provided by Rudebusch, Sack, and Swanson (2007) who show that a decline in the term premium of 10-year Treasury yields tends to boost GDP growth. Gilchrist, Yankov, and Zakrajšek (2010) who study the transmission of credit spread shocks to the broader economy within a structural framework, demonstrate that an unexpected widening of credit spreads leads to a significant contraction of economic activity and a fall in prices. Eickmeier and Hofmann (2012) also show that a contractionary term spread shock that raises the yield spread lowers output and prices.

The sign restrictions we propose to recover the ‘pure’ spread shock are in line with these stated policy objectives and previous empirical evidence that a compression in the spread should lead to higher levels of economic activity and exert upward pressure on inflation. However, the very nature of the question we are trying to answer—‘*What are the macroeconomic effects of a spread compression in a situation in which the central bank leaves the policy rate unchanged?*’—commands that the spread shock cannot possibly be recovered *via* sign restrictions alone, but requires a zero restriction on the impact response of the short-term interest rate. To extract the structural shock to the yield spread, we propose a novel identification strategy that combines sign restrictions with a single zero restriction on impact. A key point to stress is that, for the present purpose, the identification of a ‘pure’ spread shock—pure in the sense that it does not trigger a policy response—is of crucial importance, since it allows us to explore the impact of a compression of the yield spread within an environment in which the policy rate is bound to stay unchanged for an extended period. During normal times, the pure spread shock can be thought of as any unexpected disturbance in financial markets to which the central bank does not feel compelled to respond to on impact. Examples of this type of shock include shifts in liquidity preferences, in long-term inflation expectations, and in investor’s risk appetite and flight-to-quality considerations.

In addition, we identify three ‘traditional’ shocks—monetary policy, demand non-policy, and supply—*via* a standard set of sign restrictions (see, e.g., Benati 2008; Benati and Good-

hart 2010).<sup>5</sup> Even though we are not genuinely interested in these three shocks given that our focus is on the pure spread shock, Canova and Paustian (2011) and Kilian and Murphy (2012) make the case that in order to pin down the shock of interest all theoretically plausible restrictions ought to be imposed. While the responses of the spread after the supply and demand non-policy shocks are left unrestricted, postulating a flattening of the yield curve after a contractionary monetary policy shock can be motivated by imperfect pass-through along the term structure of interest rates given that short-term interest rates are only temporarily higher.

The contemporaneous restrictions on the responses of the short-term interest rate, the yield spread, inflation and output growth characterizing each structural shock are summarized in Table 1. It can be shown that this set of restrictions is sufficient to separate the various shocks from one another, thus achieving identification.

Table 1: Identification restrictions

Variable:	Shock:			
	$\epsilon_t^{MP}$	$\epsilon_t^{Spread}$	$\epsilon_t^{Demand}$	$\epsilon_t^{Supply}$
<i>Short rate</i>	+	0	+	?
<i>Spread</i>	−	−	?	?
<i>Inflation</i>	−	+	+	−
<i>Output growth</i>	−	+	+	+

? = left unconstrained

We compute the time-varying structural impact matrix,  $A_{0,t}$ , by combining the procedure proposed by Rubio-Ramírez, Waggoner, and Zha (2010) for imposing sign restrictions<sup>6</sup> with the imposition of a single zero restriction *via* a deterministic rotation matrix. Specifically, let  $\Omega_t = P_t D_t P_t'$  be the eigenvalue-eigenvector decomposition of the VAR's time-varying covariance matrix  $\Omega_t$ , and let  $\tilde{A}_{0,t} \equiv P_t D_t^{\frac{1}{2}}$ . We draw an  $N \times N$  matrix,  $K$ , from the  $N(0, 1)$  distribution, we take the  $QR$  decomposition of  $K$ —that is, we compute matrices  $Q$  and  $R$  such that  $K = Q \cdot R$ —and we compute the time-varying structural impact matrix as  $\bar{A}_{0,t} = \tilde{A}_{0,t} \cdot Q'$ . We then impose a zero in the (1, 2) position of  $\bar{A}_{0,t}$  *via* an appropriate rotation of  $\bar{A}_{0,t}$ . Specifically, by defining a rotation matrix  $\bar{R}$  as

$$\bar{R} = \left[ \begin{array}{cc|c} \cos(\varphi) & -\sin(\varphi) & 0_2 \\ \sin(\varphi) & \cos(\varphi) & \\ \hline & 0_2 & I_2 \end{array} \right] \quad (11)$$

<sup>5</sup>See also Faust (1998), Canova and De Nicolò (2002) and Uhlig (2005). A key advantage of sign restrictions is that they are, in principle, fully compatible with general equilibrium models, while this is not necessarily the case for alternative identification schemes based on, e.g., exclusion restrictions (see Canova and Pina 2005).

<sup>6</sup>See <http://home.earthlink.net/~tzha02/ProgramCode/SRestrictRWZalg.m>.

with  $\bar{R} \cdot \bar{R}' = I_4$  where  $I_4$  is a  $4 \times 4$  identity matrix. The rotation angle  $\varphi$  is defined as  $\varphi = \tan^{-1}(\bar{A}_{0,t}^{1,2}/\bar{A}_{0,t}^{1,1})$ , where  $\tan$  stands for tangens and  $\bar{A}_{0,t}^{i,j}$  denotes the  $(i,j)$  element of the candidate impact matrix  $\bar{A}_{0,t}$  at time  $t$ , such that we obtain a new impact matrix  $A_{0,t} = \bar{A}_{0,t} \cdot \bar{R}$  that has a zero in the  $(1,2)$  position. If  $A_{0,t}$  satisfies the sign restrictions we keep it, otherwise we discard it. We repeat this procedure until we obtain an impact matrix that fulfils both the sign restrictions and the zero restriction at the same time.

### 3 Evidence on the Impact of a Compression in the Yield Spread

In this section, we provide empirical evidence for the two questions posed in the introduction. First, conditional on available estimates of the impact of central banks' asset purchase programs on long-term government bond yield spreads, what role did unconventional monetary policy actions play within the context of the 2007-2009 Great Recession? In particular, did the large-scale asset purchase programs instituted by the Federal Reserve and the Bank of England avert substantial risks of deflation and of output contractions, on a scale comparable to those which took place during the Great Depression? Second, how large is the impact of a compression in the long-term yield spread on inflation and output growth within an environment in which the short-term policy rate does not move, because—in the present context—it is constrained by the zero lower bound, and has that impact changed over time? Before addressing these issues in turn, we assess the plausibility of our baseline model by looking at the dynamic effects of a conventional monetary policy tightening over time.

#### 3.1 Responses to a conventional monetary policy shock

Since the reliability of our results ultimately depends upon the ability of the empirical model to accurately capture the underlying structural relationships, it is instructive to get an idea about how well our model performs along a dimension that has been studied extensively in the literature. Therefore, a useful starting point for the analysis of the effects of unconventional monetary policy is a review of the responses to a traditional innovation in the monetary policy rule. This exercise helps ensure consistency with similar time-varying VAR models that have investigated changes in the monetary transmission mechanism.<sup>7</sup>

Figure 1, panels A and B display the time profile of the posterior median responses of inflation and of real output growth to an exogenous increase in the policy rate of 25 basis points for the U.S. and the U.K., respectively, for a period of 10 quarters after the

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<sup>7</sup>Note that this comparison is useful also because we added the stochastic volatility component in the law of motion of the VAR coefficients which was absent in previous structural TVP studies about the transmission mechanism.

contractionary monetary policy shock. We observe that the negative effect of a monetary tightening of equal size on inflation and on output growth becomes gradually stronger over the sample period in both economies. In particular, discretionary monetary policy in the U.S. induces a greater decline in real economic activity over time, while in the U.K. inflation falls by more since the introduction of the inflation-targeting regime. Both variables exhibit the largest responses during the past couple of years. These results are in line with previous evidence presented in Canova and Gambetti (2009) and Benati and Mumtaz (2007) for the U.S. and in Benati (2008) for the U.K. The finding of a substantial drop in inflation and in output growth in response to a monetary policy contraction since the onset of the crisis cautions against recommending raising interest rates to stir inflation expectations as a strategy to exit the liquidity trap as advocated by, e.g., Schmitt-Grohé and Uribe (2010) since such a policy is likely to exacerbate current economic conditions.

## 3.2 Did unconventional monetary policies avert catastrophic outcomes?

### 3.2.1 The United States

It would seem that unconventional central bank interventions in the Treasury market during 2009 should be readily reflected in the sequence of estimated structural shocks to the government bond yield spread. Figure 2 plots the historical series of pure spread shocks where the vertical line marks the first announcement of the large-scale asset purchase program by the Federal Reserve (Fed). As can be seen from the graph, spread shocks were mainly *positive* during the first round of asset purchases. This observation can be explained by the fact that spread shocks during 2009 were not just the result of central bank interventions, but also determined by crisis-related factors that were pushing up the spread. Specifically, the key motivation for conducting non-standard monetary policy operations was precisely that there were countervailing forces such as the drying up of liquidity, panic and strains on financial markets etc., which were exerting upward pressures on the yield spread. This implies that simply looking at the sequence of pure spread shocks is uninformative about what the spread would have been in the absence of central banks' asset purchases and hence, suppressing those shocks does not constitute a valid counterfactual to gauge the macroeconomic implications of unconventional policy measures.

One way to quantify whether unconventional monetary policy actions have reduced the threat of deflation and counteracted even larger output contractions is to generate a hypothetical sequence of spread shocks that undo the impact of quantitative easing policies on the term spread to obtain a counterfactual path for inflation and real GDP growth had the asset purchases not taken place.<sup>8</sup> In their extensive empirical analysis of the effect of

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<sup>8</sup>See, e.g., Sims and Zha (2006) for a similar counterfactual analysis in relation to changes in the conduct of conventional monetary policy.

the Fed’s asset purchase programs on U.S. long-term yield spreads, Gagnon *et al.* (2011) conclude that

‘[...] these purchases caused economically meaningful and long-lasting reductions in longer-term interest rates on a range of securities, including securities that were not included in the purchase programs. [...] Our results [based on time-series methods] suggest that the \$1.725 trillion in announced purchases reduced the 10-year term premium by between 38 and 82 basis points. This range of point forecasts overlaps considerably with that obtained in our event study, which is impressive given that entirely separate data and methodologies were used to obtain the results.’

D’Amico and King (2010) find that the program as a whole resulted in a downward shift of the yield curve of about 50 basis points in the 10-15 year maturity segment. Chung *et al.* (2012) derive a long-run trajectory for the evolution of the effects of asset purchases on the yield spread that die out only gradually over the years based on a portfolio-balance model. While appealing, we adopt the simplifying assumption that the central bank intervenes in such a way as to maintain the initial effects over the lifetime of the program. This is consistent with evidence provided by D’Amico and King (2010). Furthermore, given the long horizons considered by Chung *et al.* (2012), the steady decline in term-premium effects amounts only to a couple of basis points difference in the short run.

In what follows, we take Gagnon *et al.*’s (2011) time-series estimates as our benchmark measure of the impact of the Fed’s asset purchases on U.S. long-term yield spreads—specifically, for illustrative purposes, we will consider the average between their lower and upper estimates of the impact on the 10-year government bond yield spread, that is 60 basis points<sup>9</sup>—and we will tackle the question of what would have happened if the Fed had not engineered such a yield spread compression *via* asset purchases. Specifically, we ask whether the U.S. economy would have fallen into prolonged deflation like Japan in the 1990s and whether the output collapse would have been as severe as during the Great Depression.

Figure 3, panel A, reports the results from the following counterfactual simulation. Starting in 2009Q1, we re-run history

(i) conditional on the time-varying VAR’s estimated coefficients,

(ii) keeping all the structural shocks except the one to the spread unchanged at their estimated historical values, and

(iii) recompute the shocks to the spread such that the counterfactual path for the spread is, for the whole of 2009, 60 basis points higher than the actual historical path.<sup>10</sup>

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<sup>9</sup>Bomfim and Meyer (2010) also estimate the total impact of the asset purchases on the 10-year Treasury yield to amount to 60 basis points.

<sup>10</sup>An important point to stress about this counterfactual simulation is that, since we are only manipulating

The first and last columns of the figure report the medians and the 16<sup>th</sup> and 84<sup>th</sup> percentiles of the distributions of the counterfactual paths for inflation and real GDP growth, together with actual inflation and real GDP growth, respectively, whereas the middle column shows the fraction of draws from the posterior distribution for which the economy is in deflation. The figure portrays a sobering picture of what might have happened had the Fed not engineered yield spread compressions *via* its asset purchase program. Specifically, based on the median estimates, macroeconomic performance would clearly have been worse, with inflation slipping one percentage point below zero, and output growth reaching a trough of minus 10 percent in the first quarter of 2009. These findings are in line with the results obtained by Chung *et al.* (2012), who also provide evidence of substantial beneficial effects on inflation and real economic activity as a result of diminished long-term bond yields.

What is especially noteworthy in panel A of Figure 3, however, are not the median projections, but rather the *risks* associated with such projections as measured by the probability of falling into the tails of the posterior distribution (see Kilian and Manganelli 2007). In particular, with regard to inflation, the fraction of draws for which counterfactual inflation would have been negative peaks at about 90 per cent in 2009Q2, and stays consistently around 80 percent over the next quarter before falling slightly below 20 percent. As for output growth, results are even more ominous, with the lower percentile reaching *minus 20 percent*. Although these figures may appear wildly implausible, it is important to keep in mind that in the fourth quarter of 1929 U.S. real GNP contracted, on a quarter-on-quarter annualized basis, by a remarkable *17.5 percent*, whereas over the three subsequent years (from 1930Q1 to 1932Q4) the average quarter-on-quarter annualized rate of growth was equal to *minus 10.4 percent*.<sup>11</sup> So, although the results portrayed in Figure 3, panel A, are outside the bounds of advanced countries' post-WWII experience, they are definitely *not* outside the bounds of historical experience; to the contrary, they are *exactly* in line with the experience of the U.S. Great Depression.

Rather, it is even possible to make a case that such counterfactual simulations paint an excessively optimistic picture of policy inactiveness. Consider the case of demand non-policy shocks. The estimated sequence of these shocks for 2009 is conditional on the Fed having announced and implemented its asset purchase program, which, among other things, contributed to 'calm nerves' and to steady markets. Had the Fed instead stood idle in face of the crisis, business and consumer confidence would have deteriorated further and would have collapsed eventually which in turn would most likely have led to a 'worse' sequence of demand non-policy shocks, and consequently, to worse macroeconomic performance across the board. This point has also been stressed by Chung *et al.* (2012) who suggest that simulation results may underestimate the beneficial effects of the program if the very existence of the program contributed to reduce concerns about extremely adverse tail events thereby boost-

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structural shocks, while leaving all other elements of the estimated SVAR unchanged, such a counterfactual is *not* vulnerable to Sargent's (1979) criticism of SVAR-based policy counterfactuals.

<sup>11</sup>These figures are based on the real GNP data found in Balke and Gordon (1986), Appendix B, Table 2.

ing household and business confidence in a way not captured in the model. We therefore conjecture that, rather than being unrealistically dire, our counterfactual scenario might in fact be *too rosy*, and that economic conditions might have turned even worse.

Given the considerable amount of uncertainty surrounding the estimates of financial market effects of the first round of asset purchases, it is instructive to assess the range of macroeconomic implications for the weakest and the strongest impact of policy interventions on yield spreads reported in the literature. Based on a term structure model, Hamilton and Wu (2012) find that the Fed’s non-standard open-market operations reduced the 10-year Treasury yield by 13 basis points which represents the lowest end of spectrum, while Neely (2010) using an event-study methodology arrives at an estimated effect of large-scale asset purchases on the 10-year government bond yield of -107 basis points. The first two columns of Figure 3, panel B, display a counterfactual ‘corridor’ for inflation and real GDP growth based on the median of the counterfactual paths obtained with the smallest and largest estimates for spread compressions.

There has been a lot of discussion about the deterioration of labor market conditions in the aftermath of the financial crisis. Therefore, we replace real GDP growth by the unemployment rate as an indicator of economic activity and evaluate how the unemployment rate would have evolved in the absence of the large-scale asset purchases. The last column of Figure 3, panel B, depicts the median counterfactual path for the unemployment rate together with the 16<sup>th</sup> and 84<sup>th</sup> percentiles of the posterior distribution, as well as the actual unemployment rate. It clearly emerges that the labor market performance would have been much worse for an extended period had the Fed not intervened since the counterfactual path for unemployment is consistently above its observed value. This evidence is consistent with Chung *et al.* (2012) who report that the unemployment rate is 0.75 percentage points lower as a result of the implementation of the program.

Thus, while not being able to lift up the economy on the same growth path that prevailed in the pre-crisis period, our results indicate that quantitative easing measures worked as an engine for economic recovery and helped guard against prolonged deflation.

### 3.2.2 The United Kingdom

Even though we already established for the case of the U.S. that the sequence of historical spread shocks cannot be deemed a reliable guide to assess the effectiveness of unconventional monetary policy operations, for completeness Figure 4 displays the series of pure spread shocks for the U.K. where the vertical line indicates the announcement of quantitative easing by the Bank of England (BoE). Interestingly, the shocks during the period of the policy intervention are rather small by historical standards which would suggest that quantitative easing measures and countervailing forces were more balanced.

Nevertheless, as before, we proceed by conditioning our counterfactual simulations of the

macroeconomic effects on previous estimates of the compression in the spread as a result of quantitative easing. In a speech delivered in May 2009, the Bank of England's Deputy Governor, Charlie Bean, thus spoke of the impact of the Bank's asset purchase program on long-term yield spreads:

'There are signs that these measures are having a beneficial impact [...]. Spreads on commercial paper eligible for purchase have fallen by around  $\frac{1}{2}$  percentage point and the size of the market has increased by around 10%. Similarly, average spreads on sterling investment grade corporate bonds for industrial companies have declined by some 60 basis points and gross issuance of bonds by UK companies has been strong. These developments may reflect a range of influences, but feedback from market participants suggests that our purchases have indeed played a helpful role.'

His assessment is supported by empirical evidence presented in Meier (2009) who purports that the BoE's purchases of UK government bonds have reduced gilt yields by a range of at least 35-60 basis points and by Joyce *et al.* (2011) who arrive at estimates for the financial market effects of up to 100 basis points.

Figure 5, panel A, shows the results for the U.K. from the same counterfactual exercise we discussed earlier, in which we re-run the U.K. Great Recession based on the estimated SVAR, but recompute the spread shocks for 2009 in such a way that the counterfactual path for the spread is 50 basis points higher than it has been historically. Unsurprisingly, the results are in line with those for the U.S. with strong deflation of around 4 percent based on median estimates and a severe recession with real GDP growth reaching about minus 18 percent in the first quarter of 2009. Figure 5, panel B, displays the lower and upper bounds for the median estimates of the counterfactual paths for inflation and output growth conditional on the lowest (35 bp) and highest (100 bp) estimated decline in gilt yields as a result of quantitative easing. Once again, it is possible to make a convincing argument that these projections are actually optimistic in that they might understate the adverse macroeconomic outcomes absent policy interventions, exactly for the same reason previously highlighted for the U.S. We conclude that asset purchases were successful at counteracting the further weakening of real economic activity and at deflecting the threat of deflation also in the U.K.

### **3.3 How powerful is a compression in the yield spread at the zero lower bound?**

In what follows, we study the propagation of pure spread shocks under the assumption that the zero lower bound is binding for eight quarters after the spread compression. Given that a zero restriction on the nominal short-term rate is imposed only contemporaneously, we

will force the policy rate to remain unchanged for eight quarters after the impact of the spread shock when computing the impulse responses. This implies that agents expect the zero bound to constrain conventional monetary policy for a period of two years. According to Del Negro *et al.* (2010), this is a reasonable assumption for the duration of the constraint as it is in line with survey evidence of market participants during the crisis. Swanson and Williams (2012) show that the private sector has consistently expected the constraint to be binding for about one year into the future even though the zero lower bound on the policy rate has been in place now for over three years.

We employ two methodologies to take the zero lower bound constraint into account. The first approach shuts down the endogenous response of the central bank by ‘zeroing out’ the coefficients in the structural interest rate rule, while the second approach computes a sequence of hypothetical monetary policy shocks that exactly offsets the interest rate increase triggered by the expansionary spread shock.

### 3.3.1 ‘Zeroing out’ the structural interest rate rule

To examine the transmission of pure spread shocks at the zero lower bound, we subject the long-term yield spread to a one-time shock equal to minus one percent, but do not allow the short-term rate to react both on impact—which is implied by the very way we extract such ‘pure’ spread shocks—and over the subsequent eight quarters. We implement this additional restriction on the short-term interest rate by setting to zero all the coefficients in the structural VAR’s monetary policy rule, with the exception of the one on the short rate itself. To fix ideas, let the structural time-varying parameter VAR (henceforth, TVP-SVAR) representation be given by

$$A_{0,t}^{-1}Y_t = A_{0,t}^{-1}B_{1,t}Y_{t-1} + \dots + A_{0,t}^{-1}B_{p,t}Y_{t-p} + \epsilon_t \quad (12)$$

where  $Y_t \equiv [R_t, X_t']'$  is an  $N \times 1$  vector of endogenous variables, with  $R_t$  being the nominal short-term rate and  $X_t$  being an  $(N - 1) \times 1$  vector of variables other than  $R_t$ , including the spread, inflation, and real output growth;  $A_{0,t}$  being the impact matrix of the structural shocks at time  $t$ ;  $B_{1,t}, \dots, B_{p,t}$  being the time-varying autoregressive matrices of the VAR; and  $\epsilon_t = A_{0,t}^{-1}u_t$  being a vector collecting the VAR’s structural innovations where  $u_t$  is the  $N \times 1$  vector containing the VAR’s reduced-form shocks. The vector  $\epsilon_t$  is defined as  $\epsilon_t \equiv [\epsilon_{R,t}, \epsilon'_{-R,t}]'$ , where  $\epsilon_{R,t}$  is the conventional monetary policy shock, and  $\epsilon_{-R,t}$  is a vector collecting all the structural shocks other than  $\epsilon_{R,t}$ . Define  $\tilde{B}_{0,t} \equiv A_{0,t}^{-1}$ ,  $\tilde{B}_{1,t} \equiv A_{0,t}^{-1}B_{1,t}$ , ...,  $\tilde{B}_{p,t} \equiv A_{0,t}^{-1}B_{p,t}$ , and partition  $\tilde{B}_{0,t}, \tilde{B}_{1,t}, \dots, \tilde{B}_{p,t}$  as

$$\tilde{B}_{0,t} = \begin{bmatrix} \tilde{B}_{0,t}^R \\ \tilde{B}_{0,t}^{-R} \end{bmatrix}, \tilde{B}_{1,t} = \begin{bmatrix} \tilde{B}_{1,t}^R \\ \tilde{B}_{1,t}^{-R} \end{bmatrix}, \dots, \tilde{B}_{p,t} = \begin{bmatrix} \tilde{B}_{p,t}^R \\ \tilde{B}_{p,t}^{-R} \end{bmatrix}. \quad (13)$$

Leaving the short-term rate unchanged after the impact period is achieved by ‘zeroing out’ the relevant elements of the matrices  $\tilde{B}_{0,t}$ ,  $\tilde{B}_{1,t}$ , ...,  $\tilde{B}_{p,t}$  in (13) as follows:

$$\tilde{B}_{0,t}^* = \left[ \begin{array}{c} \tilde{B}_{0,t,11}^R \quad 0_{1 \times (N-1)} \\ \tilde{B}_{0,t}^{\sim R} \end{array} \right], \tilde{B}_{1,t}^* = \left[ \begin{array}{c} 0_{1 \times N} \\ \tilde{B}_{1,t}^{\sim R} \end{array} \right], \dots, \tilde{B}_{p,t}^* = \left[ \begin{array}{c} 0_{1 \times N} \\ \tilde{B}_{p,t}^{\sim R} \end{array} \right] \quad (14)$$

where  $\tilde{B}_{0,t,11}^R$  is the (1,1) element of  $\tilde{B}_0$  at time  $t$ . The dynamics of the system after the initial impact is then described by the reduced-form VAR implied by  $\tilde{B}_{0,t}^*$ ,  $\tilde{B}_{1,t}^*$ , ...,  $\tilde{B}_{p,t}^*$ . From the ninth quarter after the impact onwards, we allow the TVP-SVAR’s monetary rule to ‘kick in’, and hence use the original matrices  $B_{1,t}$ , ...,  $B_{p,t}$ , rather than those implied by  $\tilde{B}_{0,t}^*$ ,  $\tilde{B}_{1,t}^*$ , ...,  $\tilde{B}_{p,t}^*$ .

Figures 6 and 8 show, for the U.S. and the U.K., the median time-varying impulse response functions (henceforth, IRFs) of the policy rate, the yield spread, GDP deflator inflation, and real GDP growth, to an unexpected decrease in the spread of 100 basis points for the entire sample period. Figures 7 and 9 on the other hand, show, for the same countries and variables, the median IRFs to a one-percent negative shock to the yield spread together with the 16<sup>th</sup> and 84<sup>th</sup> percentiles of the posterior distribution for selected quarters.

Several findings are readily apparent from these figures. In particular, the IRFs of the spread itself to a negative one-percent shock exhibit little time variation. On the contrary, evidence of time variation is, in general, quite substantial for both inflation and real GDP growth, thus providing both a strong justification for the use of time-varying estimation methods, and an important *caveat* to results obtained with fixed-coefficient models. This is especially apparent for the responses of U.S. inflation and real GDP growth, which since the end of the 1960s have exhibited three peaks around the time of the Great Inflation of the 1970s, of the recession of the early 1990s, and in the most recent past. These results clearly suggest that a fixed-coefficient model estimated over (say) the last two decades will understate the impact on inflation and output growth of a compression in the yield spread during the financial crisis, as this sample period mixes two sub-samples which, in this respect, are quite different. Evidence of gradual time variation is even more apparent for the U.K. for both inflation and output growth. In particular, for both variables the impact of a compression in the yield spread appears to have increased in recent years. Finally—and crucially, for the present purposes—the stimulative power on both inflation and output growth of a reduction in the spread appears to be substantial. For the U.S. in 2009Q4, for example, real GDP growth increased (based on median estimates) by 1.2 percent in the quarter of impact, it peaks at 2.2 percent three quarters after the impact, and it then rapidly fades away over subsequent quarters. The impact on inflation starts at 0.4 percent on impact, it peaks at 1.7 percent after three quarters, and it then decreases. The results for the U.K. are quantitatively slightly different but are, overall, of the same order of magnitude.

It is important to be mindful of the fact that constructing any counterfactual simulation is subject to the Lucas critique since it is based on the notion of taking an estimated SVAR and

changing (some of) the parameters in its structural monetary policy rule which in the present context amounts to setting them to zero (see Sargent 1979). As shown by Benati and Surico (2009) by means of a single example based on an estimated standard New Keynesian model, and as extensively analyzed by Benati (2010) based on a battery of estimated DSGE models, the results produced by such counterfactuals may turn out to be misleading. Therefore, in the next section, we perform the exercise under consideration by manipulating the monetary policy shocks, rather than the coefficients of the SVAR’s monetary policy rule.

### 3.3.2 ‘Constant-interest-rate’ projection methodology

An alternative way to obtain IRFs to a spread shock when the zero lower bound is assumed to be binding for eight quarters after impact is to construct a sequence of monetary policy shocks that exactly neutralizes the systematic component of monetary policy which would require raising the short-term rate in response to higher inflation and real output growth triggered by the spread compression, thereby keeping the short-term rate constant over this period. This method is routinely used in central banks in order to compute ‘constant-interest-rate’ (henceforth, CIR) projections. From the ninth quarter onwards, we again allow the short rate to move according to what is dictated by the SVAR’s monetary policy rule.

Figures 10 and 11 display for the U.S. and the U.K., respectively, the time-varying median IRFs obtained with this methodology. The results for the U.K. are remarkably similar to those produced with the earlier approach. The IRFs for U.S. inflation and output growth exhibit a greater volatility for several quarters, but are however, in the same ballpark as those reported in Figure 6. Compared with the results obtained by ‘zeroing out’ the coefficients of the SVAR’s interest rate rule, the IRFs derived with the CIR methodology display considerable volatility, which can be attributed to the workings of the following ‘feedback loop’. On impact, a compression of the spread stimulates output growth and inflation. As a consequence, starting from the first quarter after the impact the SVAR’s monetary rule would call for an increase in the policy rate in order to temper such expansionary effects. The negative monetary policy shock that we inject to offset such a rise of the short rate exerts a *further* expansionary effect on inflation and real GDP growth, thereby compounding the initial impact of the spread shock. Therefore, depending on (i) how large the impact of a spread shock is on inflation and on output growth, and (ii) how strongly monetary policy responds to higher inflation and output growth, this feedback loop may lead to highly volatile IRFs. On the other hand, in the limiting case in which the policy rate does not react to inflation and output growth, the feedback loop would not even ‘kick in’, and the problem would not exist. This implies that this problem is not a general one, but rather may or may not be there depending on the specific structure of the economy at each point in time.

Even though this way of imposing the zero lower bound is not vulnerable to the Lucas critique in the strict sense since we are only manipulating monetary policy shocks and not the coefficients of the structural VAR’s interest rate rule, there are however other implications for

agents' expectations. First, since the structural monetary policy rule which is encoded in the estimated SVAR implies that the short-term rate always reacts to the state of the economy, this exercise ignores the direct effect on expectations formed by the public of the central bank's announcement that it will keep the interest rate unchanged for an 'extended period'.<sup>12</sup> This expectational channel has the potential to amplify the macroeconomic consequences of a compression in the yield spread. Second, it is assumed that the public will not revise the model it uses to forecast the future path of the nominal interest rate despite the fact that the policy rate is consistently deviating in one direction—downwards—from the path that would be implied uniquely by the systematic component of monetary policy as a result of a sequence of interest rate 'surprises' *all of the same sign*. If, instead, agents were to notice that policy shocks are no longer drawn from a zero-mean, symmetric distribution, but from a distribution with an upper bound at zero, they would use this information when generating their interest rate forecasts. Whether the public will or will not detect such a pattern eventually depends on (*i*) how large these shocks are and (*ii*) how long the shock sequence lasts. In the present case, it is not evidently unreasonable to presume that the public will not readily uncover such a systematic pattern given that the surprise changes in the interest rate last for a comparatively short period.

### 3.3.3 On the sources of time variation

As previously discussed, based on both methodologies we detect significant time variation in the economy's response to a compression in the yield spread. Although identifying the *sources* of such time variation is clearly beyond the scope of this paper, one possible cause deserves to be at least briefly mentioned.<sup>13</sup> Historically, changes in the yield spread for a given short rate have had a multiplicity of causes: shifts in long-term inflation expectations, changes in the liquidity premium, etc. Since it is at least possible to entertain the hypothesis that different underlying causes of changes in the yield spread may lead to a different pattern of responses of the economy—that is, to different impulse response functions to a compression of the yield spread of a given magnitude—one obvious possibility for the identified changes over time in the pattern of IRFs is that such changes may simply result from a change in the 'mixture' of the underlying shocks leading to changes in the yield spread. We consider this an interesting avenue for future research.

### 3.3.4 Normal times versus zero lower bound episode

In sections 3.3.1 and 3.3.2, we postulated that the zero lower bound was binding throughout the sample period. We now examine the macroeconomic effects of a spread compression in

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<sup>12</sup>We say 'for an extended period' since leaving the interest rate unchanged forever, and announcing that to the public, leads to global indeterminacy.

<sup>13</sup>We wish to thank a referee for pointing this out.

the absence of a zero lower bound constraint on the policy rate as would be relevant for the pre-crisis period.

Figure 12 compares, for the U.S. (panel A) and the U.K. (panel B), the time profile of the constrained and unconstrained responses of prices and real GDP one year after the unanticipated reduction in the yield spread by one percent.<sup>14</sup> We observe that, in several historical episodes, both U.S. output and prices react more strongly to a spread compression when the policy rate is held fixed. The reason for the smaller effects in the unconstrained case is that in those periods the central bank responds to the decline in the long-short spread by raising interest rates considerably (not reported) which contains inflation and output growth. Starting in 2000, the gap between the responses with and without the zero bound in place widens for both macroeconomic variables and becomes largest during the period of large-scale asset purchases which lends support to the idea that the constraint on the policy rate magnifies the effects of a spread shock on the macroeconomy.

What is striking is that in the U.K. over the pre-crisis sample the transmission of spread shocks to the macroeconomy does not seem to be affected much by imposing the zero lower bound constraint. Whether the policy rate is allowed to react to a spread shock after impact or whether it is constrained to zero for eight consecutive quarters, has virtually no effect on output and makes only little difference for the price response before the start of quantitative easing. In contrast, the macroeconomic consequences are greatly amplified from early 2009 onwards when the zero bound was effectively binding.

## 4 Conclusions

In this paper, we have explored the macroeconomic effects of a compression in the long-term bond yield spread within the context of the Great Recession of 2007-2009 *via* a multivariate structural VAR with time-varying parameters and stochastic volatility to account for changes in the economic structure in the aftermath of the financial crisis. We have identified a ‘pure’ spread shock as a disturbance that leaves the policy rate unchanged on impact, which allowed us to characterize the macroeconomic consequences of a compression in the yield spread induced by central banks’ asset purchases within an environment in which the short-term rate cannot move because it is constrained by the zero lower bound.

Two main findings emerged from our empirical analysis. First, a compression in the long-term yield spread exerts a powerful effect on both output growth and inflation in the U.S. and in the U.K. when the zero lower bound is binding. Second, conditional on consensus estimates of the impact of the Federal Reserve’s and the Bank of England’s asset purchase programs on long-term government bond yield spreads, our counterfactual simulations have

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<sup>14</sup>The reason for choosing a one-year horizon is that agents at this point will undoubtedly have realized that the central bank is keeping the policy rate fixed. However, the results are not markedly different for shorter or longer horizons.

indicated that both in the U.S. and in the U.K. unconventional monetary policy actions have been successful at mitigating significant risks both of deflation and of further output collapses comparable to those that took place during the Great Depression. Our model simulations suggest that in the absence of policy interventions the U.S. economy would have been in deflation until 2009Q3 with annualized inflation rates as low as -1%. Real GDP would have been 0.9 percent lower, and unemployment would have been 0.75 percentage points higher reaching a level of about 10.6% in 2009Q4. Similarly, in the U.K., without quantitative easing annualized inflation would have fallen to minus 4 percent and output growth would have reached a trough of minus 12 percent at an annual rate in the first quarter of 2009 based on the median of our counterfactual estimates. Based on these results, we conclude that large-scale purchases of Treasury securities constitute a viable policy option to provide additional monetary policy accommodation in a zero lower bound environment that enable central banks to achieve their mandate of promoting price stability and, in the case of the Federal Reserve, fostering full employment and should therefore be added to the toolkit of monetary authorities.

It cannot be excluded, however, that there were additional forces at play that are not captured in our empirical model, which have the potential to reinforce the macroeconomic stimulus induced by the large open-market purchases of domestic government debt. First, unconventional fiscal policy operations in the wake of the crisis complement monetary policy efforts when the economy is stuck at the zero lower bound (see, e.g., Auerbach and Obstfeld 2005). Second, the announcement and implementation of non-standard policy measures should also have stabilizing effects on agents' expectations and contribute to a rebound of confidence that enhance the effectiveness of policy interventions. Carvalho, Cúrdia, Eusepi, and Grisse (2011), based on cross-country experiences during the crisis, present evidence that both unconventional monetary and fiscal actions positively affected the evolution of inflation and growth expectations. Exploring these and other additional channels of non-standard policy interventions is an important task for future research to provide a comprehensive assessment of the beneficial macroeconomic effects of such policies.

## A Data appendix

### A.1 United States

A monthly seasonally unadjusted series for the Federal Funds rate (FEDFUNDS) available for the period July 1954-December 2011, and a monthly series for the 10-year Treasury constant-maturity rate (GS10) available for April 1953-December 2011, are from the *St. Louis FED's FRED database*. We converted them to quarterly frequency by taking averages within the quarter. Quarterly seasonally adjusted series for real GDP (GDPC96) and the GDP deflator (GDPDEF), available for the period 1947Q1-2011Q4, are from the same database.

### A.2 United Kingdom

Quarterly seasonally adjusted series for real GDP and the GDP deflator are from the *Office for National Statistics*, and are available since the first quarter of 1955. The Treasury bill rate and the long-term government bond yield for the period 1964Q1 to 2011Q4 are from the *International Monetary Fund's International Financial Statistics* database.

## B Details of the Markov Chain Monte Carlo Procedure

We estimate the model described by equations (1)-(10) *via* Bayesian methods. The next two subsections describe our choices for the priors, and the Markov Chain Monte Carlo algorithm we use to simulate the posterior distribution of the hyperparameters and the states conditional on the data. Section 3 provides evidence for the convergence of the Markov chain to the ergodic distribution and section 4 provides an informal assessment of our modeling assumptions.

### B.1 Prior distributions and initial values

For the sake of simplicity, the prior distributions of the states— $\theta_0$ ,  $\alpha_0$ ,  $h_0$ , and  $q_0$ —which we postulate all to be normal, are assumed to be independent both from one another, and from the distribution of the hyperparameters. In order to calibrate the prior distributions for  $\theta_0$ ,  $\alpha_0$ ,  $h_0$ , and  $q_0$  and to obtain initial values, we estimate a time-invariant version of (1) based on the first 10 years of data, and we set

$$\theta_0 \sim N \left[ \hat{\theta}_{OLS}, 4 \cdot \hat{V}(\hat{\theta}_{OLS}) \right] \tag{B1}$$

As for  $\alpha_0$  and  $h_0$  we proceed as follows. Let  $\hat{\Sigma}_{OLS}$  be the estimated covariance matrix of  $\epsilon_t$  from the time-invariant VAR, and let  $C$  be the lower-triangular Choleski factor of  $\hat{\Sigma}_{OLS}$ —i.e.,  $CC' = \hat{\Sigma}_{OLS}$ . We set

$$\ln h_0 \sim N(\ln \mu_0, 10 \times I_4) \quad (\text{B2})$$

where  $\mu_0$  is a vector collecting the squared elements on the diagonal of  $C$ . We then divide each column of  $C$  by the corresponding element on the diagonal—let's call the matrix we thus obtain  $\tilde{C}$ —and we set

$$\alpha_0 \sim N[\tilde{\alpha}_0, \tilde{V}(\tilde{\alpha}_0)] \quad (\text{B3})$$

where  $\tilde{\alpha}_0$ —which, for future reference, we define as  $\tilde{\alpha}_0 \equiv [\tilde{\alpha}_{0,11}, \tilde{\alpha}_{0,21}, \dots, \tilde{\alpha}_{0,61}]'$ —is a vector collecting all the non-zero and non-unity elements of  $\tilde{C}^{-1}$  (i.e, the elements below the diagonal), and its covariance matrix,  $\tilde{V}(\tilde{\alpha}_0)$ , is postulated to be diagonal, with each individual  $(j,j)$  element equal to 10 times the absolute value of the corresponding  $j$ -th element of  $\tilde{\alpha}_0$ . Such a choice for the covariance matrix of  $\alpha_0$  is clearly arbitrary, but is motivated by our goal to scale the variance of each individual element of  $\alpha_0$  in such a way as to take into account of the element's magnitude.

As for  $q_0$  we proceed as follows. Let  $Q_0$  be the prior matrix for the extent of random-walk drift of the VAR's parameters  $\theta_t$  that we would use if we were working with a traditional Bayesian time-varying parameters VAR with a *constant* extent of random-walk drift over the sample. We set  $Q_0 = \gamma \times \hat{\Sigma}_{OLS}$ , with  $\gamma = 1.0 \times 10^{-4}$ , the same value used in Primiceri (2005), and a relatively 'conservative' prior for the extent of drift compared (e.g.) to the  $3.5 \times 10^{-4}$  used by Cogley and Sargent (2002). We set

$$\ln q_0 \sim N(10^{-2} \times \ln \bar{q}_0, 10 \times I_{N \cdot (1+N_p)}) \quad (\text{B4})$$

where  $\bar{q}_0$  is a vector collecting the elements on the diagonal of  $Q_0$ .

Turning to the hyperparameters, we postulate independence between the parameters corresponding to the matrices  $S$  and  $Z$ —an assumption we adopt uniquely for reasons of convenience—and we make the following, standard assumptions. The three blocks of  $S$  are assumed to follow inverted Wishart distributions, with prior degrees of freedom set, again, equal to the minimum allowed, respectively, 2, 3 and 4:

$$S_1 \sim IW(\bar{S}_1^{-1}, 2) \quad (\text{B5})$$

$$S_2 \sim IW(\bar{S}_2^{-1}, 3) \quad (\text{B6})$$

$$S_3 \sim IW(\bar{S}_3^{-1}, 4) \quad (\text{B7})$$

As for  $\bar{S}_1$ ,  $\bar{S}_2$  and  $\bar{S}_3$ , we calibrate them based on  $\tilde{\alpha}_0$  in (B3) as:

$$\bar{S}_1 = 10^{-3} \times |\tilde{\alpha}_{0,11}|, \quad \bar{S}_2 = 10^{-3} \times \text{diag}([\tilde{\alpha}_{0,21}|, |\tilde{\alpha}_{0,31}|]') \quad \text{and} \quad \bar{S}_3 = 10^{-3} \times \text{diag}([\tilde{\alpha}_{0,41}|, |\tilde{\alpha}_{0,51}|, |\tilde{\alpha}_{0,61}|]').$$

Such a calibration is consistent with the one we adopted for  $Q$ , as it is equivalent to setting  $\bar{S}_1$ ,  $\bar{S}_2$  and  $\bar{S}_3$  equal to  $10^{-4}$  times the relevant diagonal block of  $\tilde{V}(\tilde{\alpha}_0)$  in (B3). As for the

variances of the innovations to the stochastic volatilities for the VAR's reduced-form shocks, we follow Cogley and Sargent (2002, 2005) and we postulate an inverse-Gamma distribution for the elements of  $Z_\nu$ ,

$$\sigma_{\nu,i}^2 \sim IG\left(\frac{10^{-4}}{2}, \frac{1}{2}\right) \quad (\text{B8})$$

Finally, as for the variances of the innovations to the stochastic volatilities for the VAR's random-walk parameters' innovations, we postulate an inverse-Gamma distribution for the elements of  $Z_\omega$ ,

$$\sigma_{\omega,i}^2 \sim IG\left(\frac{10^{-4}}{2}, \frac{10}{2}\right) \quad (\text{B9})$$

(B9) implies that the prior for  $\sigma_{\omega,i}^2$  has the same mean as in Cogley, Primiceri and Sargent (2010), but it has a smaller variance.

## B.2 Simulating the posterior distribution

We simulate the posterior distribution of the hyperparameters and the states conditional on the data *via* the following MCMC algorithm, combining elements of Primiceri (2005) and Cogley and Sargent (2002, 2005). In what follows,  $x^t$  denotes the entire history of the vector  $x$  up to time  $t$ —i.e.  $x^t \equiv [x'_1, x'_2, \dots, x'_t]'$ —while  $T$  is the sample length.

(a) *Drawing the elements of  $\theta_t$ .* Conditional on  $Y^T$ ,  $\alpha^T$ , and  $H^T$ , the observation equation (1) is linear, with Gaussian innovations and a known covariance matrix. Following Carter and Kohn (1994), the density  $p(\theta^T|Y^T, \alpha^T, H^T, V)$  can be factored as

$$p(\theta^T|Y^T, \alpha^T, H^T, V) = p(\theta_T|Y^T, \alpha^T, H^T, V) \prod_{t=1}^{T-1} p(\theta_t|\theta_{t+1}, Y^T, \alpha^T, H^T, V) \quad (\text{B10})$$

Conditional on  $\alpha^T$ ,  $H^T$ , and  $V$ , the standard Kalman filter recursions nail down the first element on the right hand side of (B10),  $p(\theta_T|Y^T, \alpha^T, H^T, V) = N(\theta_T, P_T)$ , with  $P_T$  being the precision matrix of  $\theta_T$  produced by the Kalman filter. The remaining elements in the factorization can then be computed via the backward recursion algorithm found, e.g., in Kim and Nelson (1999), or Cogley and Sargent (2005, appendix B.2.1). Given the conditional normality of  $\theta_t$ , we have

$$\theta_{t|t+1} = \theta_{t|t} + P_{t|t}P_{t+1|t}^{-1}(\theta_{t+1} - \theta_t) \quad (\text{B11})$$

$$P_{t|t+1} = P_{t|t} - P_{t|t}P_{t+1|t}^{-1}P_{t|t} \quad (\text{B12})$$

which provides, for each  $t$  from  $T-1$  to 1, the remaining elements in (1),  $p(\theta_t|\theta_{t+1}, Y^T, \alpha^T, H^T, V) = N(\theta_{t|t+1}, P_{t|t+1})$ . Specifically, the backward recursion starts with a draw from  $N(\theta_T, P_T)$ , call it  $\tilde{\theta}_T$ . Conditional on  $\tilde{\theta}_T$ , (B11)-(B12) give us  $\theta_{T-1|T}$  and  $P_{T-1|T}$ , thus allowing us to draw  $\tilde{\theta}_{T-1}$  from  $N(\theta_{T-1|T}, P_{T-1|T})$ , and so on until  $t = 1$ .

(b) *Drawing the elements of  $\alpha_t$ .* Conditional on  $Y^T$ ,  $\theta^T$ , and  $H^T$ , following Primiceri (2005), we draw the elements of  $\alpha_t$  as follows. Equation (1) can be rewritten as  $A_t \tilde{Y}_t \equiv A_t(Y_t - X_t' \theta_t) = A_t \epsilon_t \equiv u_t$ , with  $\text{Var}(u_t) = H_t$ , namely

$$\tilde{Y}_{2,t} = -\alpha_{21,t} \tilde{Y}_{1,t} + u_{2,t} \quad (\text{B13})$$

$$\tilde{Y}_{3,t} = -\alpha_{31,t} \tilde{Y}_{1,t} - \alpha_{32,t} \tilde{Y}_{2,t} + u_{3,t} \quad (\text{B14})$$

$$\tilde{Y}_{4,t} = -\alpha_{41,t} \tilde{Y}_{1,t} - \alpha_{42,t} \tilde{Y}_{2,t} - \alpha_{43,t} \tilde{Y}_{3,t} + u_{4,t} \quad (\text{B15})$$

—plus the identity  $\tilde{Y}_{1,t} = u_{1,t}$ —where  $[\tilde{Y}_{1,t}, \tilde{Y}_{2,t}, \tilde{Y}_{3,t}, \tilde{Y}_{4,t}]' \equiv \tilde{Y}_t$ . Based on the observation equations (B13)-(B15), and the transition equation (8), the elements of  $\alpha_t$  can then be drawn by applying the same algorithm we described in the previous paragraph separately to (B13)-(B15). The assumption that  $S$  has the block-diagonal structure (10) is in this respect crucial, although, as stressed by Primiceri (2005, Appendix D), it could in principle be relaxed.

(c) *Drawing the elements of  $H_t$ .* Conditional on  $Y^T$ ,  $\theta^T$ , and  $\alpha^T$ , the orthogonalised innovations  $u_t \equiv A_t(Y_t - X_t' \theta_t)$ , with  $\text{Var}(u_t) = H_t$ , are observable. Following Cogley and Sargent (2002), we then sample the  $h_{i,t}$ 's by applying the univariate algorithm of Jacquier, Polson, and Rossi (1994) element by element.<sup>15</sup>

(d) *Drawing the elements of  $Q_t$ .* Conditional on  $\theta^T$ , the innovations  $\eta_t = \theta_t - \theta_{t-1}$ , with  $\text{Var}(\eta_t) = Q_t$ , are observable, and, along the lines of point (c), we therefore sample the  $q_{j,t}$ 's by applying the univariate algorithm of Jacquier, Polson, and Rossi (1994) element by element.

(e) *Drawing the hyperparameters.* Finally, conditional on  $Y^T$ ,  $\theta^T$ ,  $H^T$ , and  $\alpha^T$ , the innovations to  $\theta_t$ ,  $\alpha_t$ , the  $h_{i,t}$ 's and the  $q_{i,t}$ 's are observable, which allows us to draw the hyperparameters—the elements of  $S_1$ ,  $S_2$ ,  $S_3$  and the  $\sigma_{\nu,i}^2$  and the  $\sigma_{\omega,i}^2$ —from their respective distributions.

Summing up, the MCMC algorithm simulates the posterior distribution of the states and the hyperparameters, conditional on the data, by iterating on (a)-(e). In what follows, we use a burn-in period of 50,000 iterations to converge to the ergodic distribution, and after that we run 10,000 more iterations sampling every  $10^{\text{th}}$  draw in order to reduce the autocorrelation across draws.

### B.3 Assessing the convergence of the Markov chain to the ergodic distribution

Following Primiceri (2005), we assess the convergence of the Markov chain by inspecting the autocorrelation properties of the draws from the ergodic distribution. Specifically, in what

<sup>15</sup>For details, see Cogley and Sargent (2005, Appendix B.2.5).

follows, we consider the draws' inefficiency factors (henceforth, IFs), defined as the inverse of the relative numerical efficiency measure of Geweke (1992),

$$RNE = (2\pi)^{-1} \frac{1}{S(0)} \int_{-\pi}^{\pi} S(\omega) d\omega \quad (\text{B16})$$

where  $S(\omega)$  is the spectral density of the sequence of draws from the Gibbs sampler for the quantity of interest at the frequency  $\omega$ . We estimate the spectral densities by smoothing the periodograms in the frequency domain by means of a Bartlett spectral window. Following Berkowitz and Diebold (1998), we select the bandwidth parameter automatically *via* the procedure introduced by Beltrão and Bloomfield (1987).

Figures 1A and 2A show, for the U.S. and the U.K., the draws' IFs for the models' hyperparameters, i.e. the free elements of the matrices  $Z_\nu$ ,  $Z_\omega$ ,  $S_1$ ,  $S_2$ , and  $S_3$ , and for the states, i.e. the time-varying coefficients of the VAR (the  $\theta_t$ 's), the volatilities of the innovations to the VAR's random-walk parameters (the  $q_{i,t}$ 's), the volatilities of the VAR's reduced-form innovations (the  $h_{i,t}$ 's), and the non-zero and non-one elements of the matrix  $A_t$ . As can be seen from the figures, for both countries the autocorrelation of the draws is uniformly very low, being in the vast majority of cases around or below 3 which suggests that the Markov chains have indeed converged.<sup>16</sup>

## B.4 An informal assessment

An informal check to assess how well our time-varying parameter VARs track the data, is to look at the inflation trends produced by the model. For the U.S., in particular, there is a vast consensus—stemming, first and foremost, from the work of Cogley and Sargent—that trend inflation peaked, during the 1970s, between 7 and 8 percent, and significantly declined since then. The estimated time-varying VAR for the U.S. should generate comparable results if our model specification performs well.

Figure 3A plots, for the U.S. (panel A) and the U.K. (panel B), actual GDP deflator inflation together with the time-varying trends generated by the model. Several things are apparent from the figures. First, concerning the U.S., the median inflation trend peaks at about 7 percent during the second half of the 1970s, exactly in line with the previous evidence. Second, the estimated inflation trends manifestly appear to capture the slow-moving, low-frequency component of inflation.

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<sup>16</sup>As stressed by Primiceri (2005, Appendix B), values of the IFs below or around twenty are generally regarded as satisfactory.

## C Computing time-varying impulse response functions

Here we describe the Monte Carlo integration procedure we use in Section 3.3 to compute nonlinear IRFs to a pure spread shock along the lines of Koop, Pesaran, and Potter (1996) and Kilian and Vigfusson (2011).

Randomly draw the current state of the economy at time  $t$  from the output of the Gibbs sampler. Given the current state of the economy, repeat the following procedure 100 times. Draw four independent  $N(0, 1)$  variates—the four structural shocks—and based on the relationship  $\epsilon_t = A_{0,t}e_t$ , with  $e_t \equiv [e_t^{MP}, e_t^{SP}, e_t^D, e_t^S]'$ , where  $e_t^{MP}$ ,  $e_t^{SP}$ ,  $e_t^D$ , and  $e_t^S$  are the monetary policy, pure spread, demand non-policy, and supply structural shocks, respectively, compute the reduced-form shocks  $\epsilon_t$  at time  $t$ . Simulate both the VAR's time-varying parameters and the covariance matrix of its reduced-form innovations,  $\Omega_t$ , 20 quarters into the future. Based on the simulated  $\Omega_t$ , randomly draw reduced-form shocks from  $t + 1$  to  $t + 20$ . Based on the simulated  $\theta_t$ , and on the sequence of reduced-form shocks from  $t$  to  $t + 20$ , compute simulated paths for the four endogenous variables. Call these simulated paths  $\hat{X}_{t,t+20}^j$ ,  $j = 1, \dots, 100$ . Repeat the same procedure 100 times based on exactly the same simulated paths for the VAR's time-varying parameters, the  $\theta_t$ ; the same reduced-form shocks at times  $t + 1$  to  $t + 20$ ; and the same structural shocks  $e_t^{MP}$ ,  $e_t^D$ , and  $e_t^S$  at time  $t$ , but setting  $e_t^{SP}$  to one. Call these simulated paths  $\tilde{X}_{t,t+20}^j$ . For each of the 100 iterations define  $irf_{t,t+20}^j \equiv \hat{X}_{t,t+20}^j - \tilde{X}_{t,t+20}^j$ . Finally, compute each of the 1,000 generalized IRFs as the mean of the distribution of  $irf_{t,t+20}^j$ .

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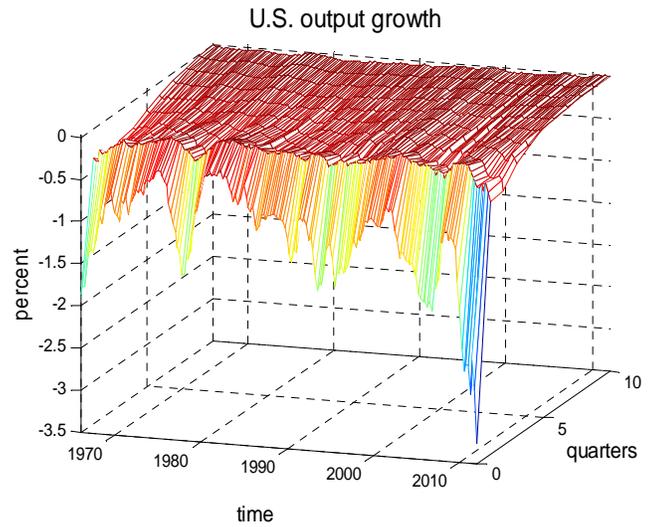
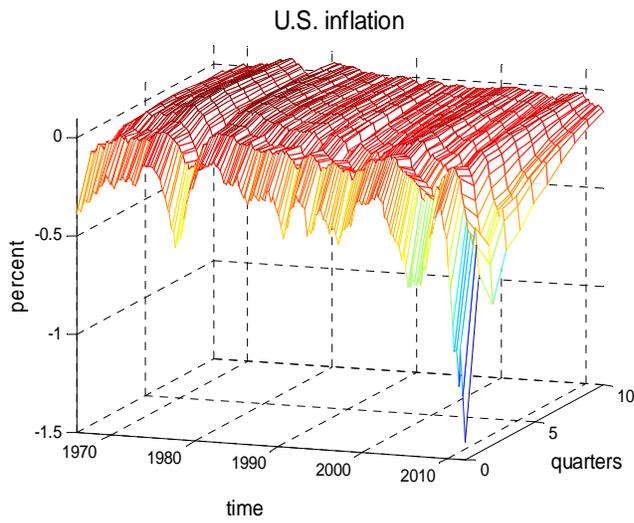
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Panel A



Panel B

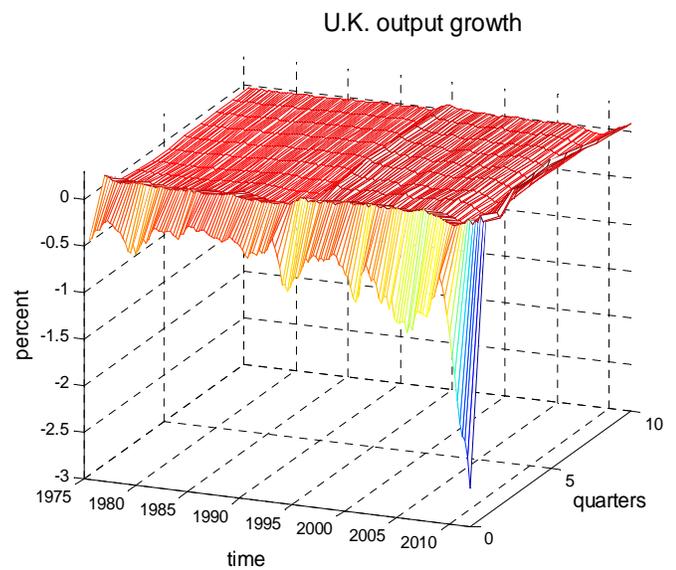
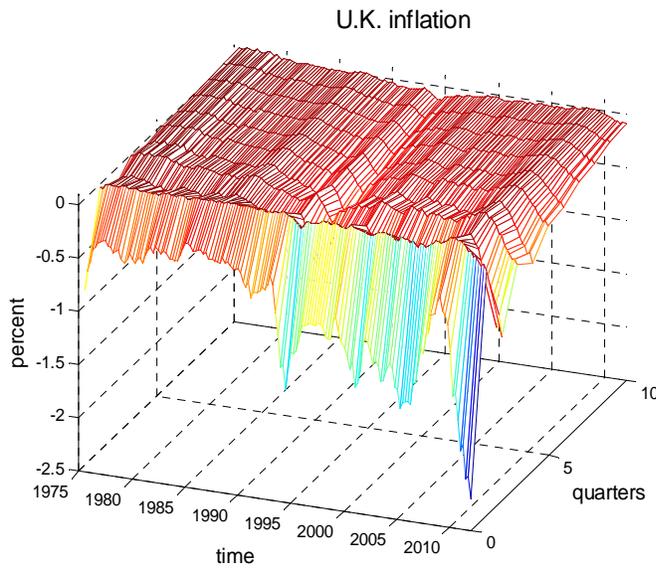


Figure 1: Time-varying median responses of inflation and output growth to a contractionary monetary policy shock of 25 basis points.

Panel A: United States over the period 1965Q1 to 2011Q4.

Panel B: United Kingdom over the period 1975Q1 to 2011Q4.

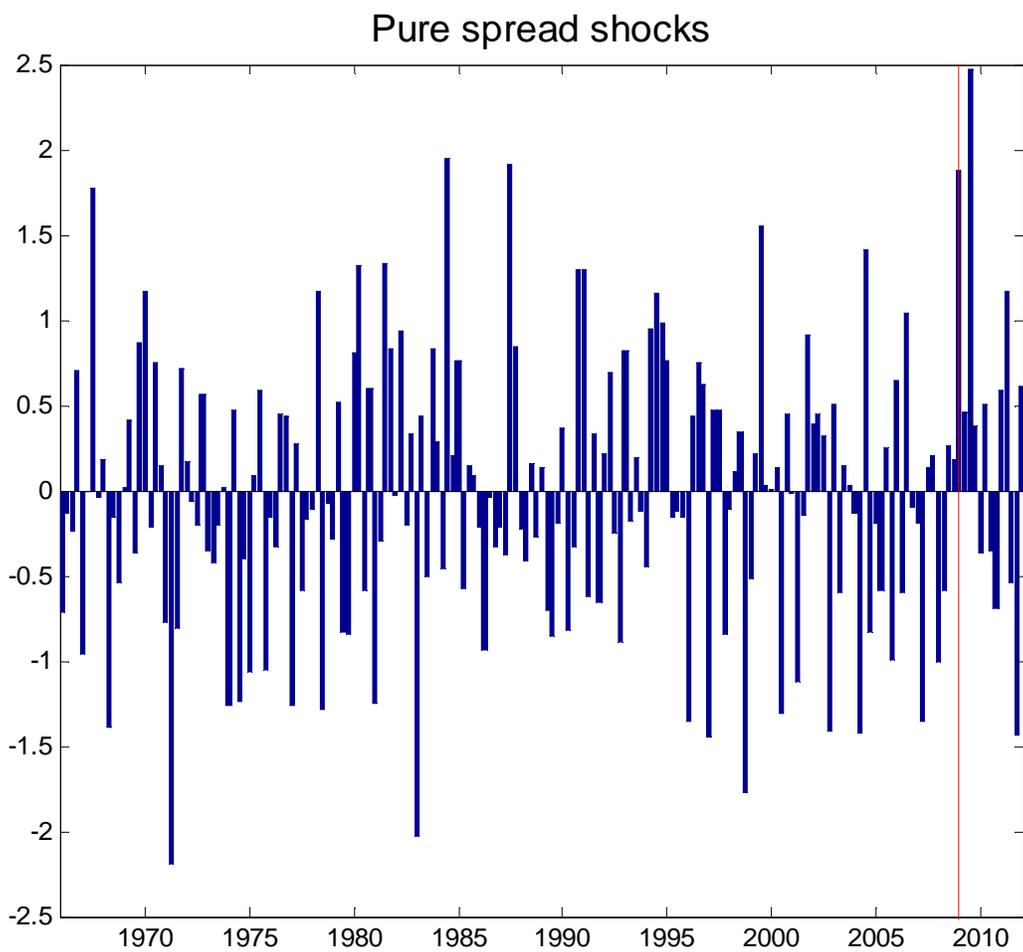
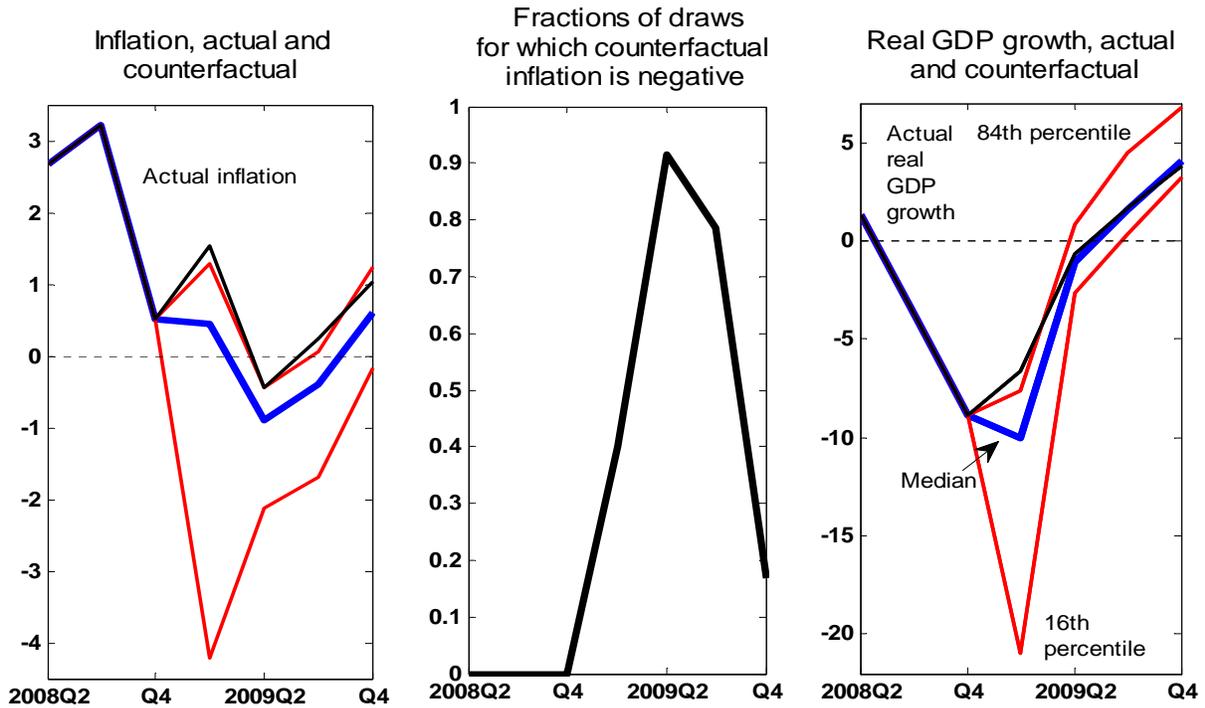


Figure 2: Historical sequence of structural shocks to the yield spread for the U.S. over the period 1965Q4 to 2011Q4 where the vertical line indicates the announcement of the large-scale asset purchase program.

Panel A



Panel B

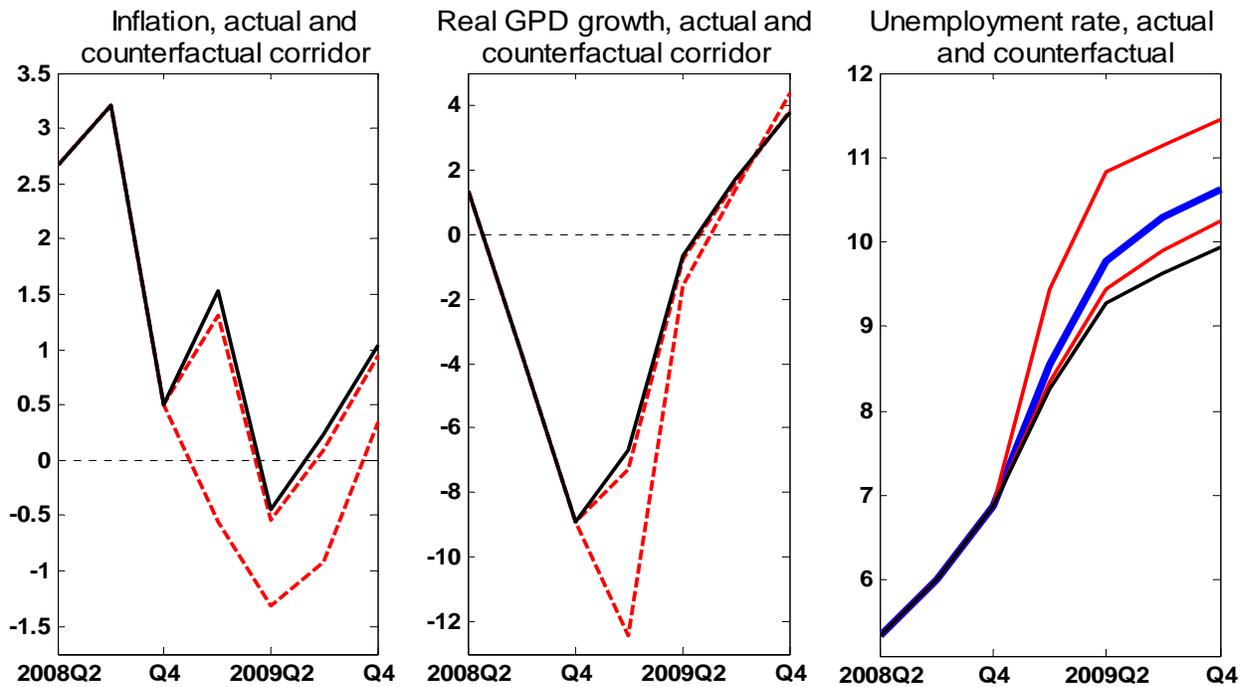


Figure 3: Counterfactual simulations for U.S. inflation, output growth and unemployment rate for 2009 eliminating the impact on the spread of the FED's asset purchases.

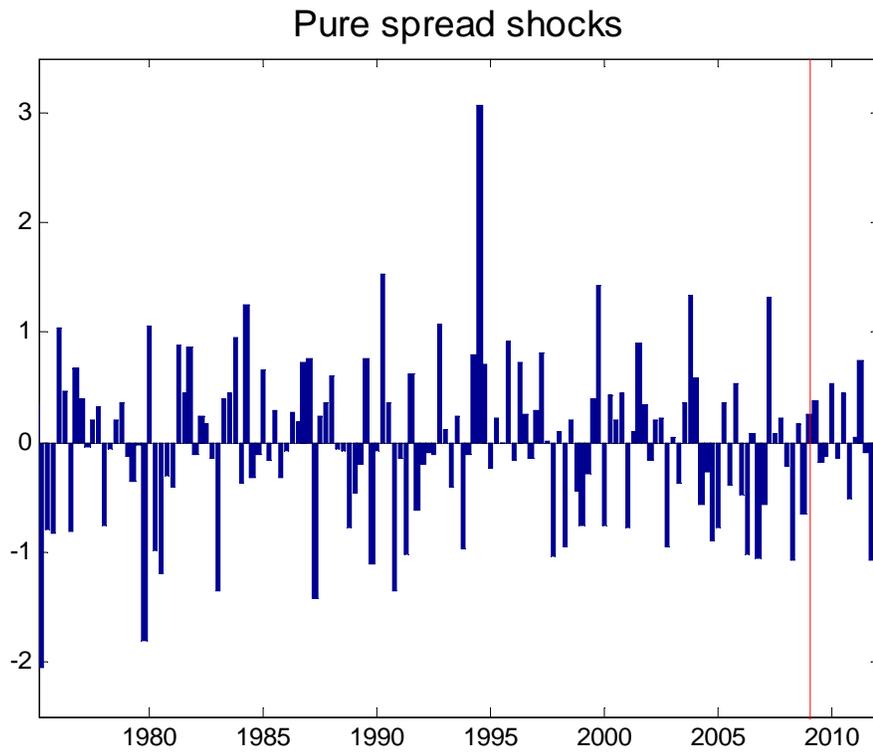


Figure 4: Historical sequence of structural shocks to the yield spread for the U.K. over the period 1975Q2 to 2011Q4 where the vertical line indicates the announcement of quantitative easing.

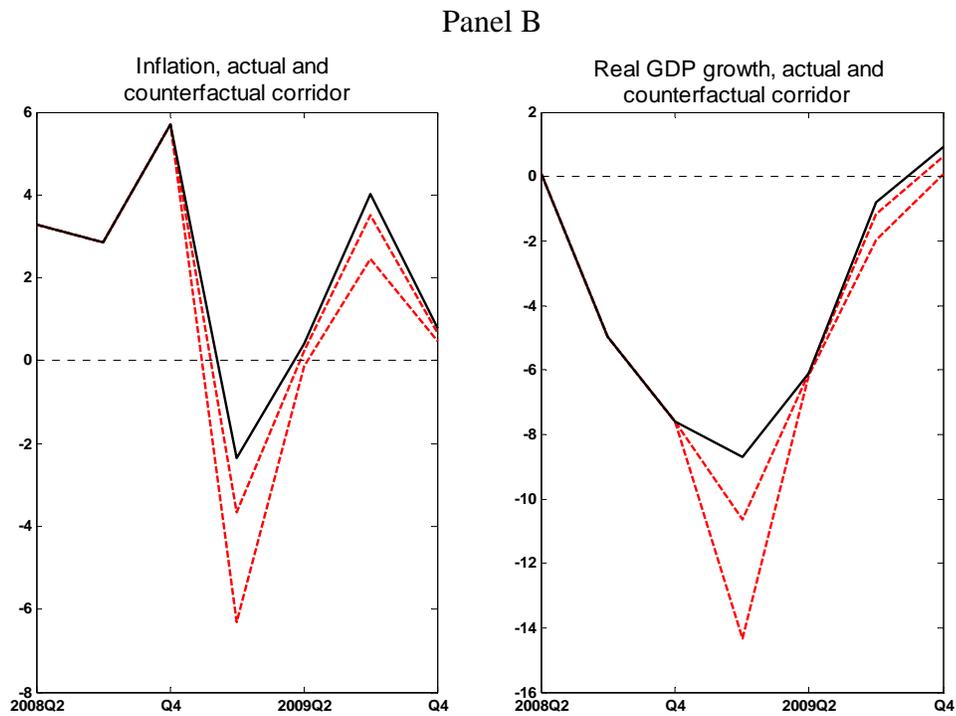
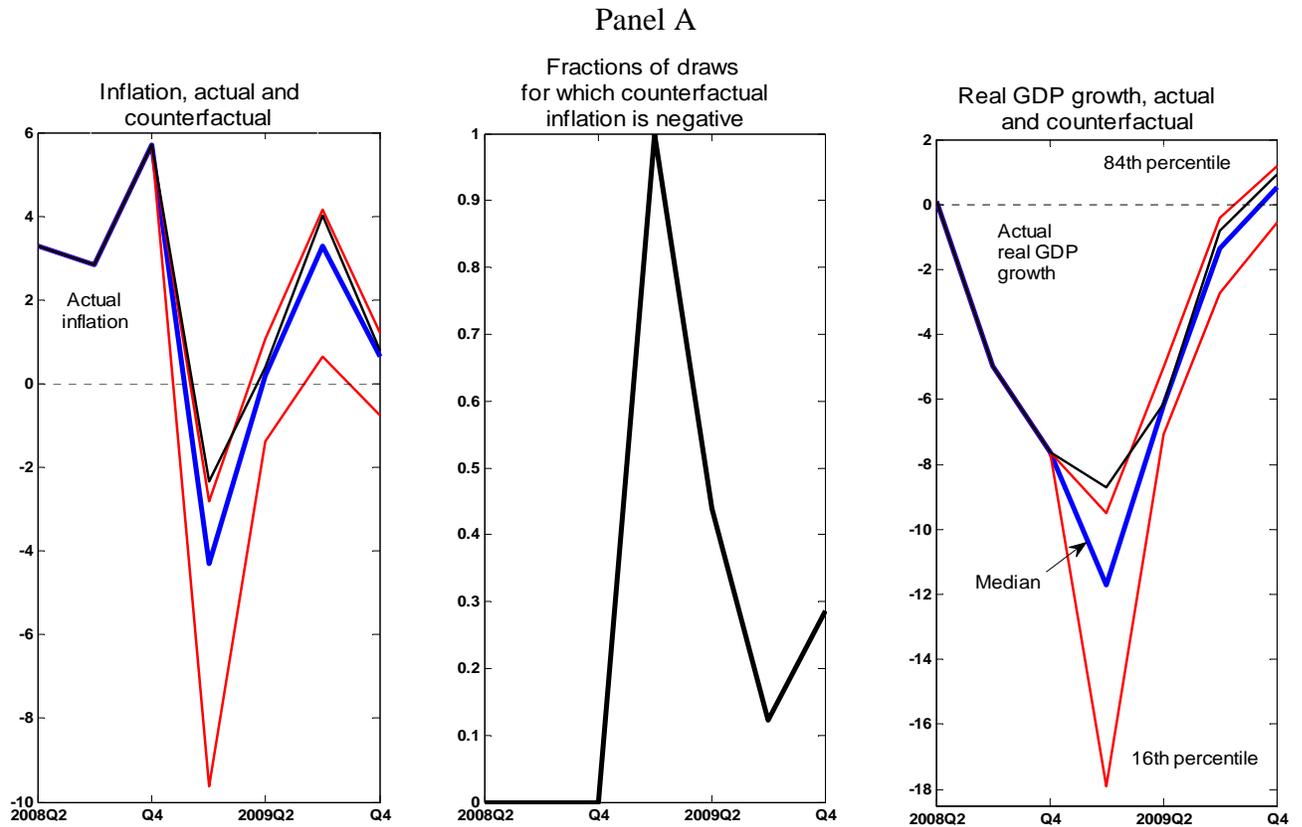


Figure 5: Counterfactual simulations for U.K. inflation and output growth for 2009 eliminating the impact on the spread of the BoE's quantitative easing measures.

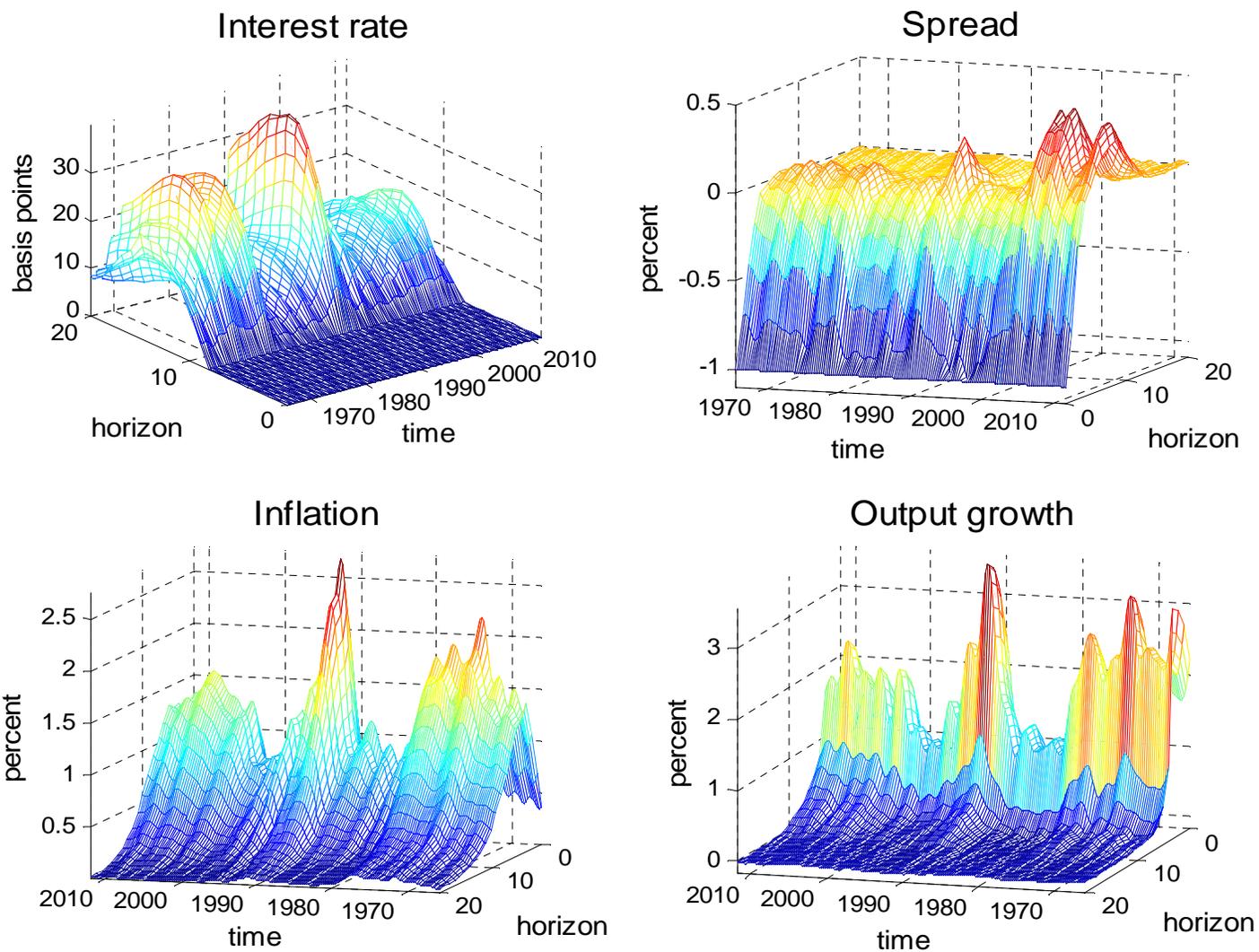


Figure 6: Median IRFs to a 1% negative shock to the long-term bond yield spread for the U.S. over the period 1965Q4 to 2011Q4 computed by setting the coefficients in the SVAR's monetary rule to zero for 8 quarters.

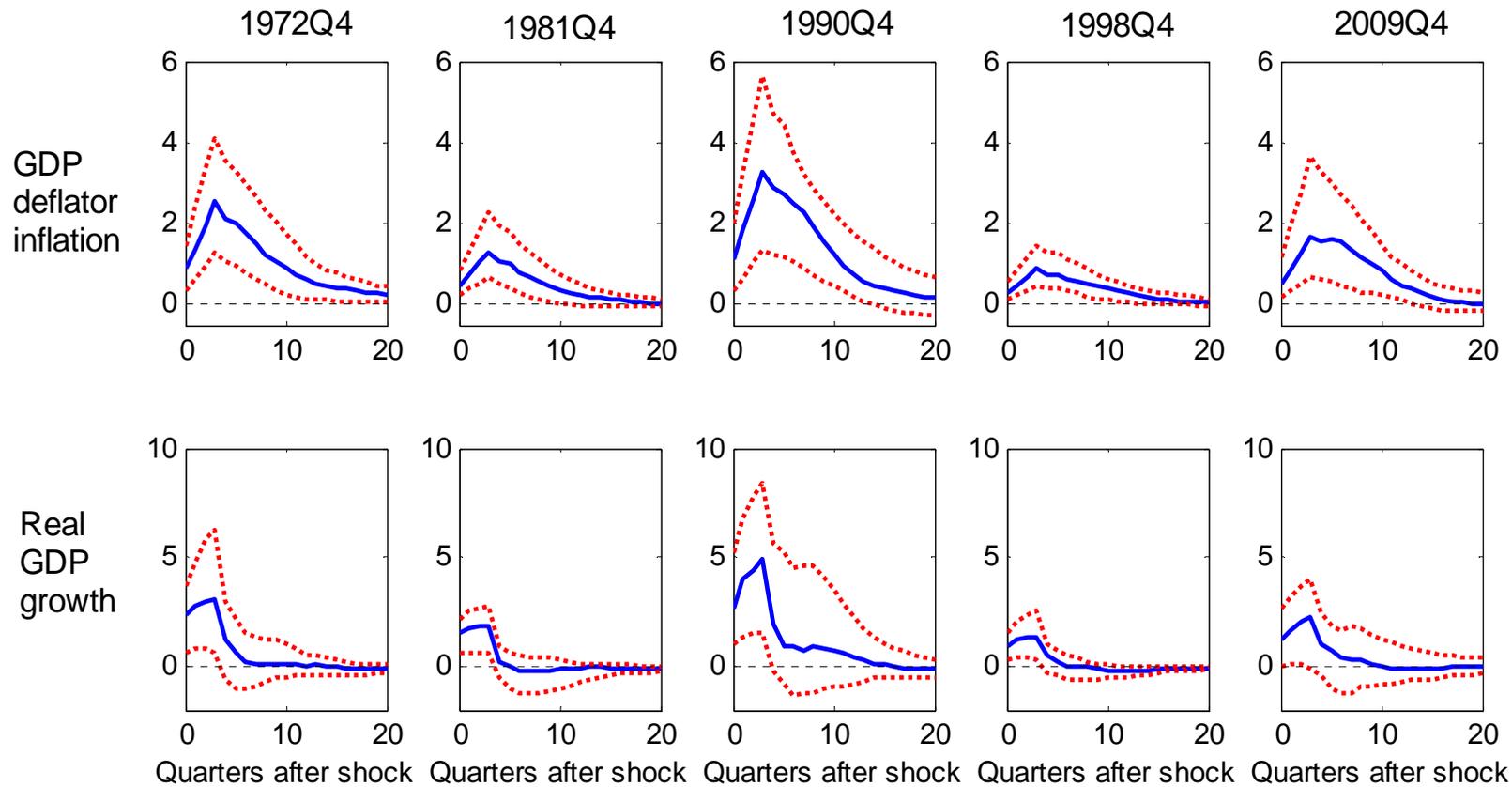


Figure 7: Median IRFs (solid lines) to a 1% negative shock to the long-term bond yield spread together with 16<sup>th</sup> and 84<sup>th</sup> percentiles (dotted lines) for the U.S. for selected quarters computed by setting the coefficients in the SVAR's monetary rule to zero for 8 quarters.

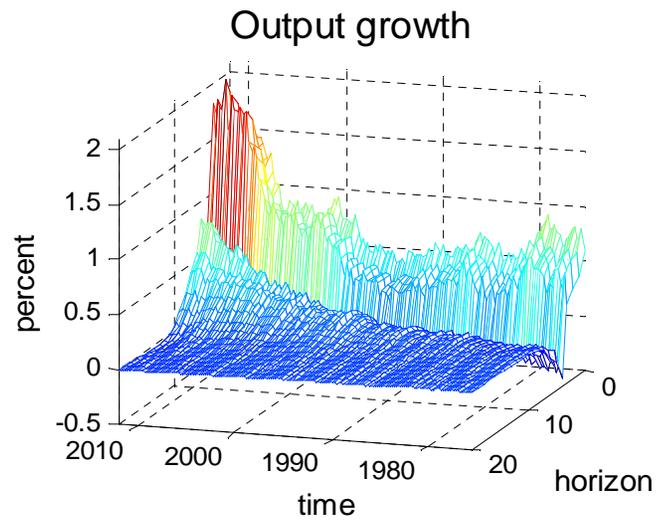
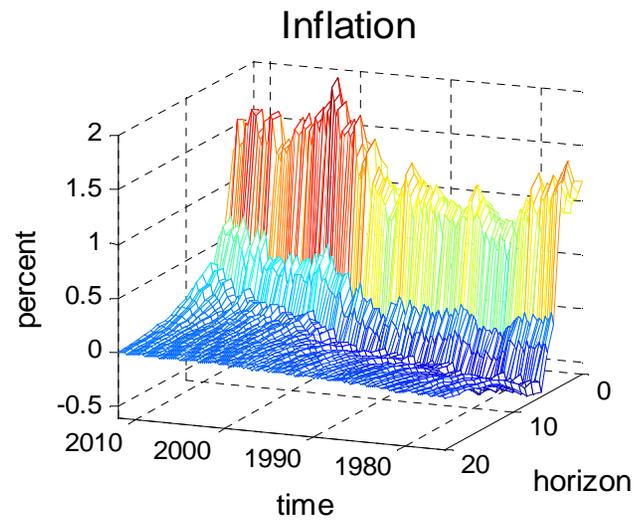
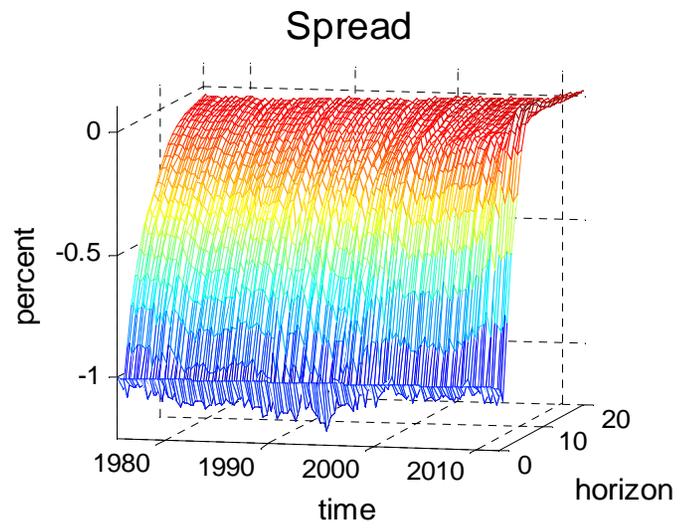
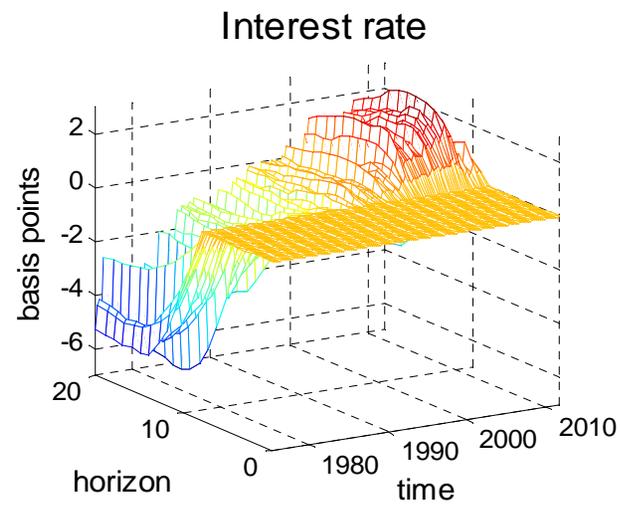


Figure 8: Median IRFs to a 1% negative shock to the long-term bond yield spread for the U.K. over the period 1975Q2 to 2011Q4 computed by setting the coefficient in the SVAR's monetary rule to zero for 8 quarters.

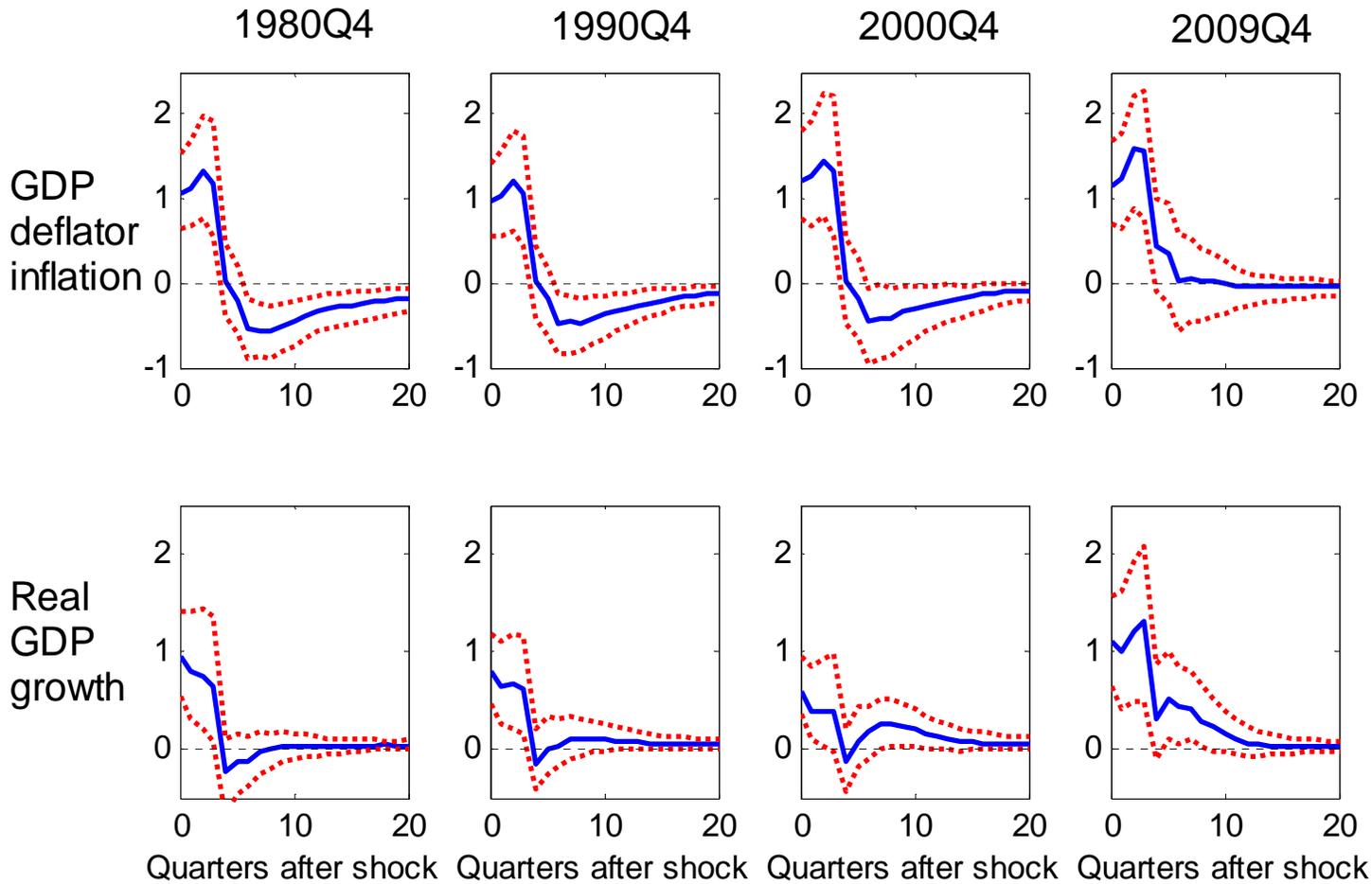


Figure 9: Median IRFs (solid lines) to a 1% negative shock to the long-term bond yield spread together with 16<sup>th</sup> and 84<sup>th</sup> percentiles (dotted lines) for the U.K. for selected quarters computed by setting the coefficients in the SVAR's monetary rule to zero for 8 quarters.

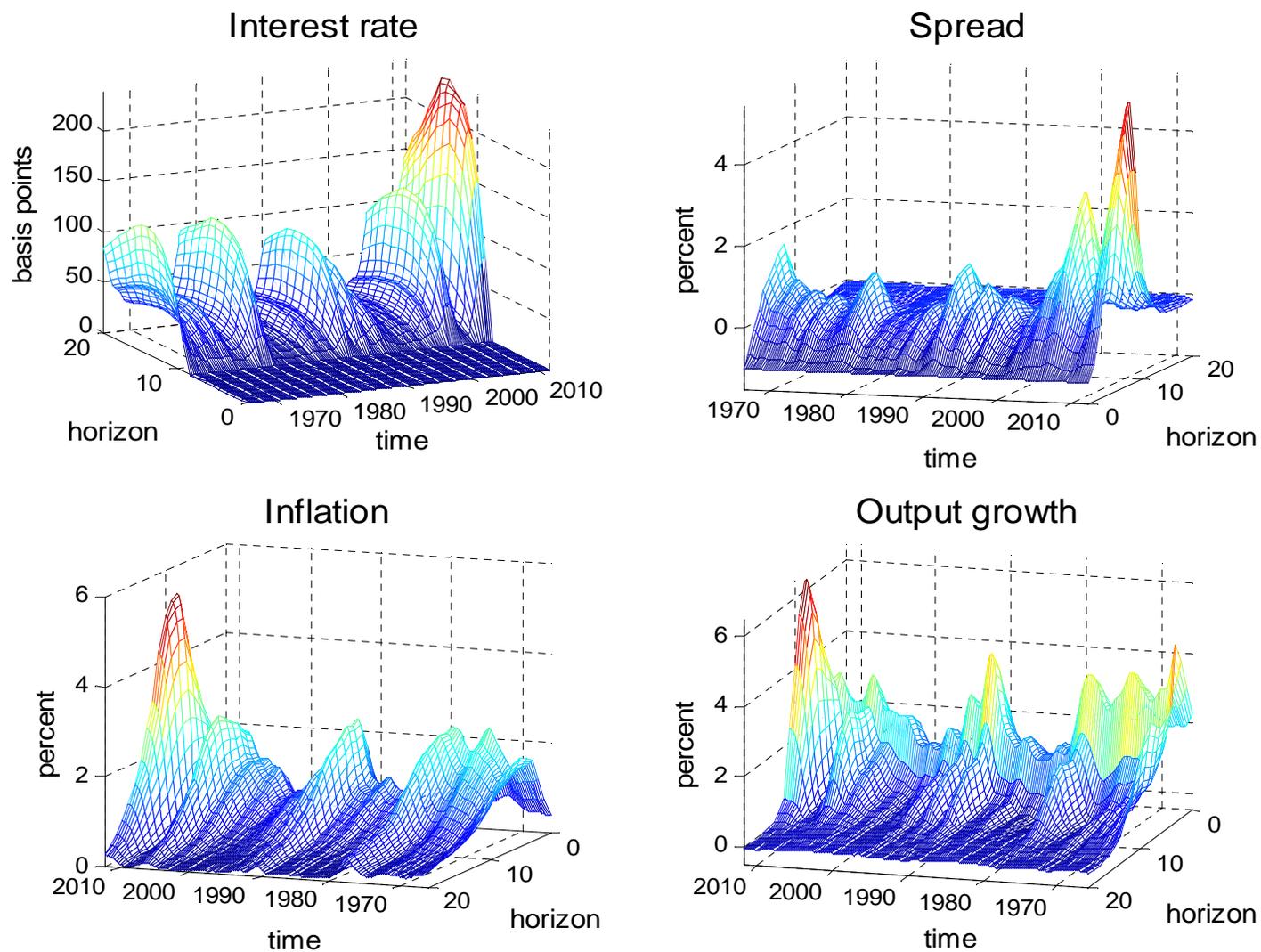


Figure 10: Median IRFs to a 1% negative shock to the long-term bond yield spread for the U.S. over the period 1965Q4 to 2011Q4 based on the ‘constant-interest-rate’ projection methodology to keep the policy rate constant for 8 quarters after impact.

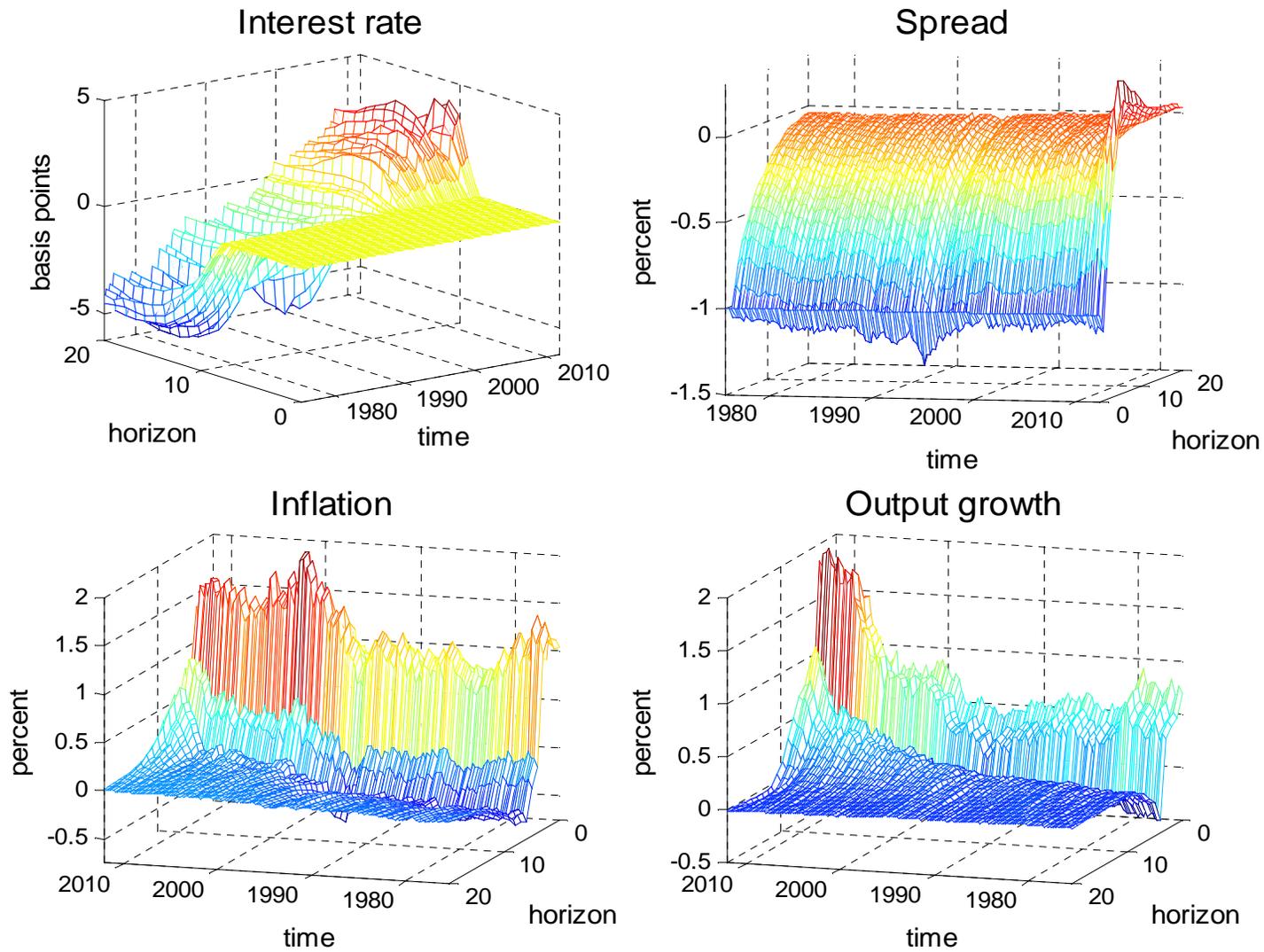
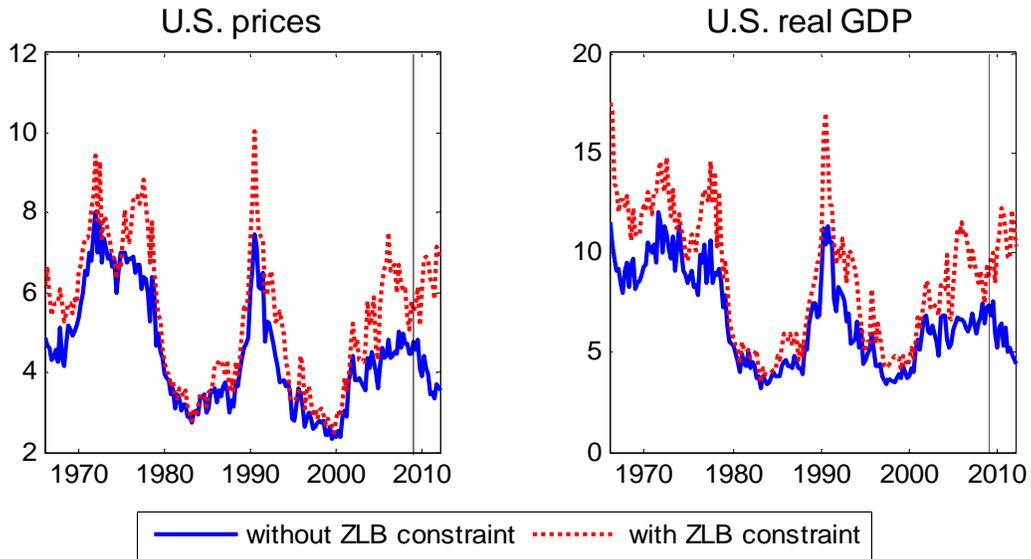


Figure 11: Median IRFs to a 1% negative shock to the long-term bond yield spread for the U.K. over the period 1975Q2 to 2011Q4 based on the ‘constant-interest-rate’ projection methodology to keep the policy rate constant for 8 quarters after impact.

Panel A



Panel B

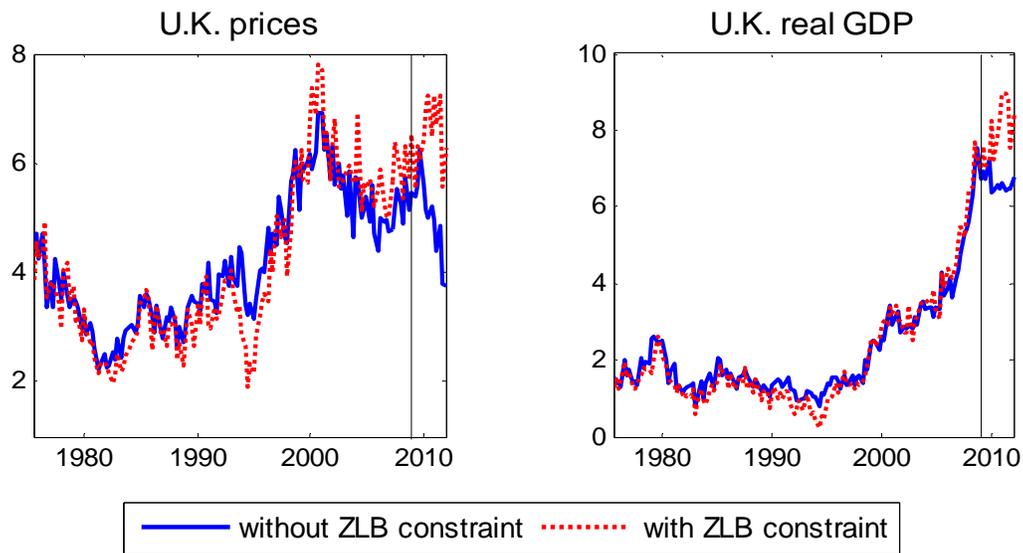


Figure 12: Time-varying median responses of inflation and real GDP one year after a 1% negative shock to the long-term yield spread with and without the zero lower bound constraint imposed on the policy rate where the vertical line indicates the start of large-scale asset purchases.

Panel A: United States over the period 1965Q4 to 2011Q4.

Panel B: United Kingdom over the period 1975Q2 to 2011Q4.

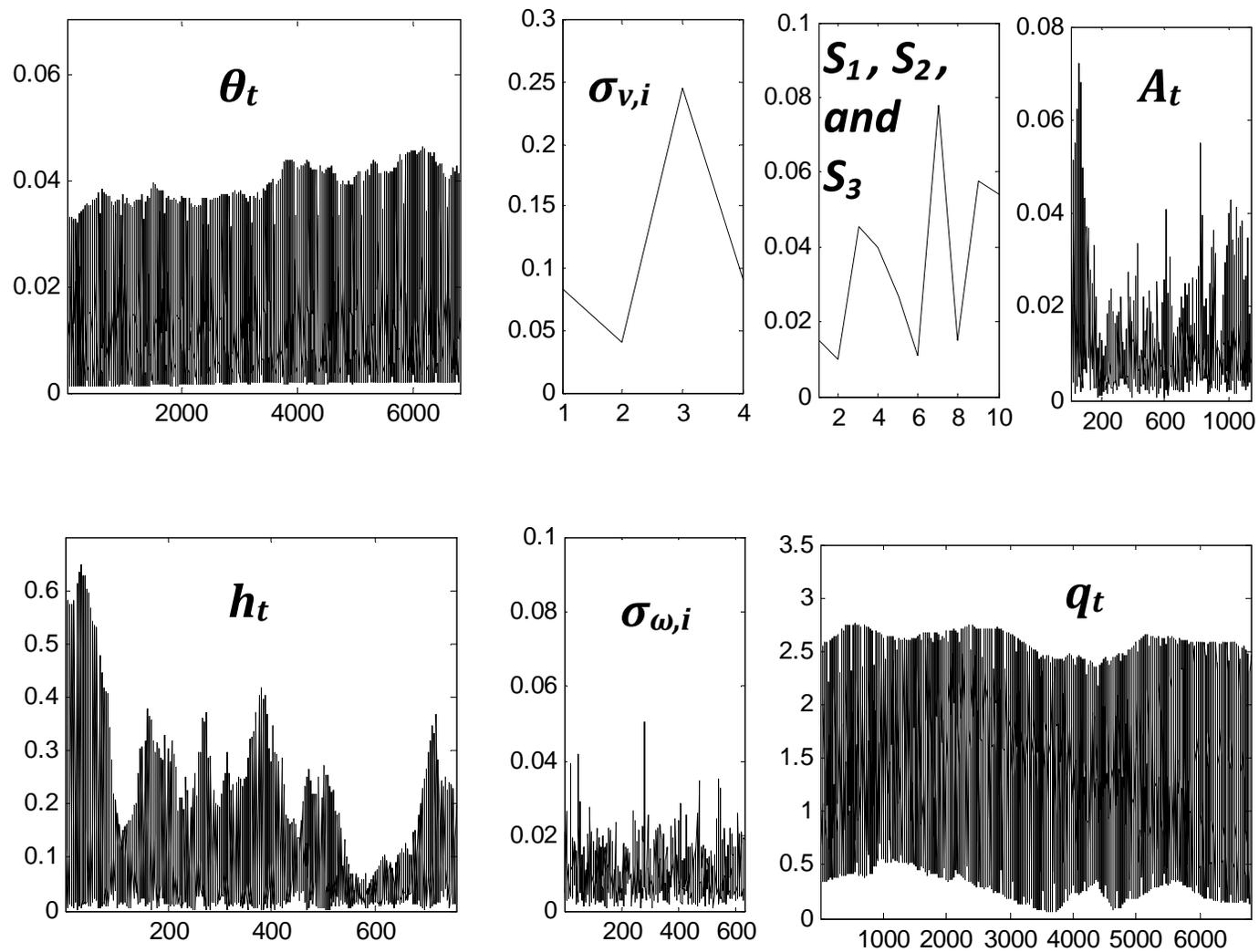


Figure 1A: Checking for convergence of the Markov chain: inefficiency factors for the draws from the ergodic distribution for the hyperparameters and the states for the U.S. VAR model.

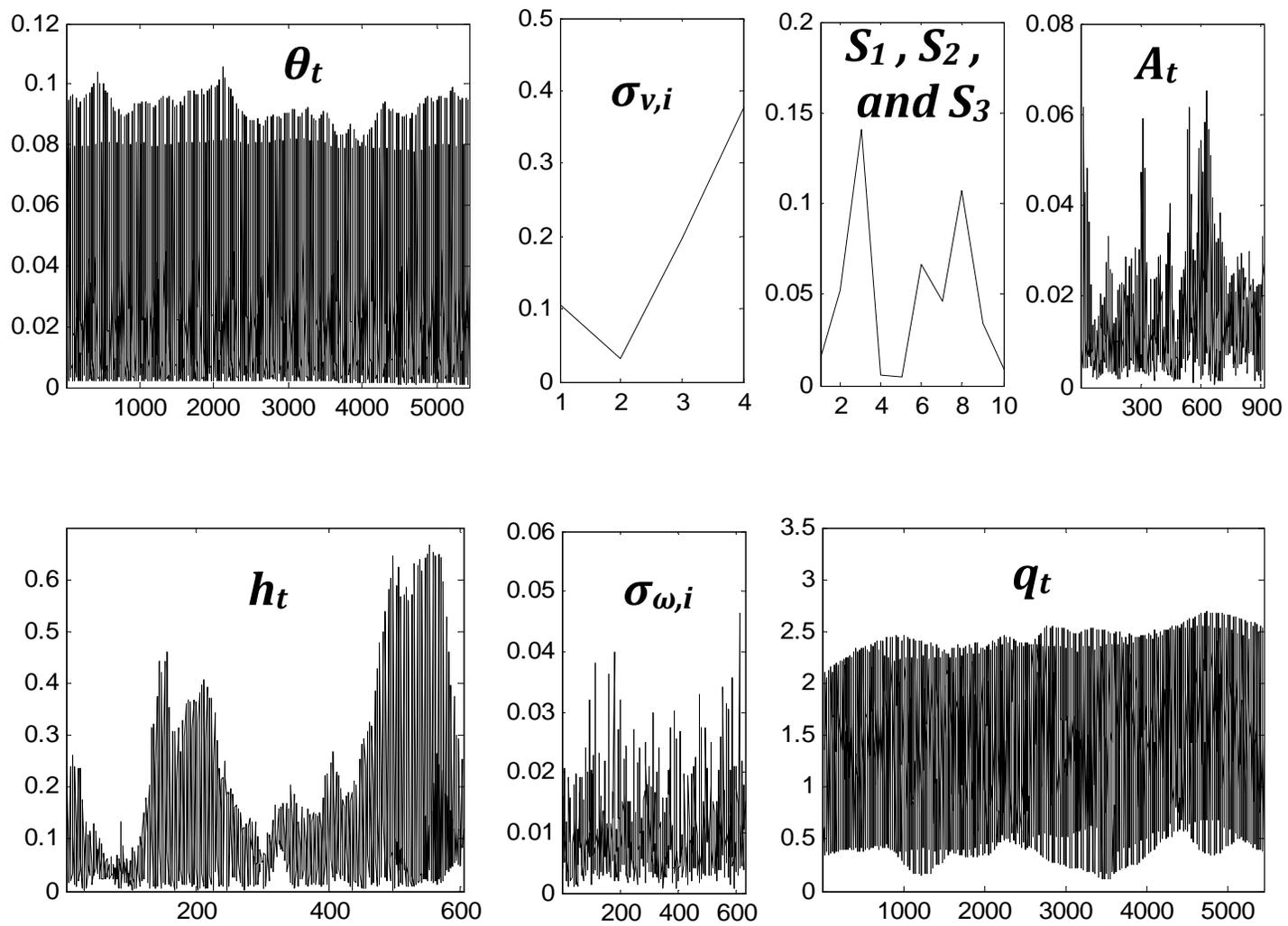


Figure 2A: Checking for convergence of the Markov chain: inefficiency factors for the draws from the ergodic distribution for the hyperparameters and the states for the U.K. VAR model.

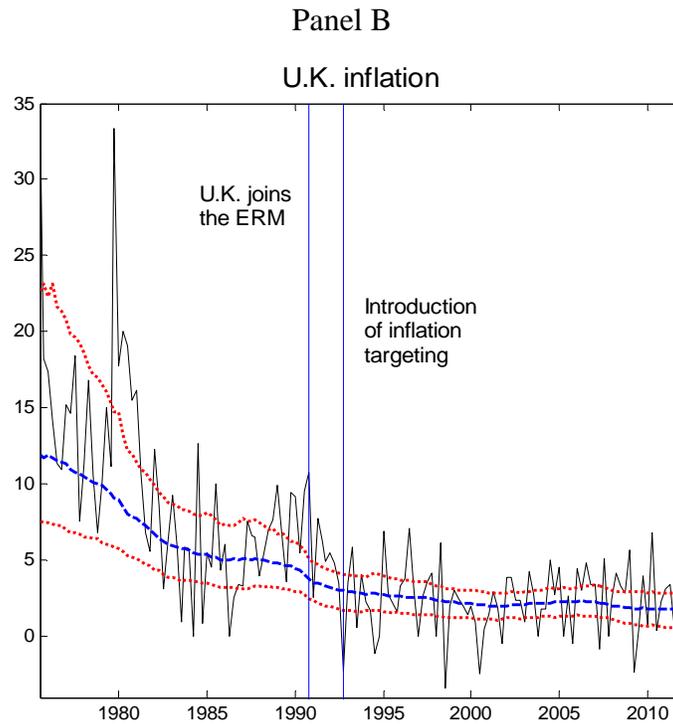
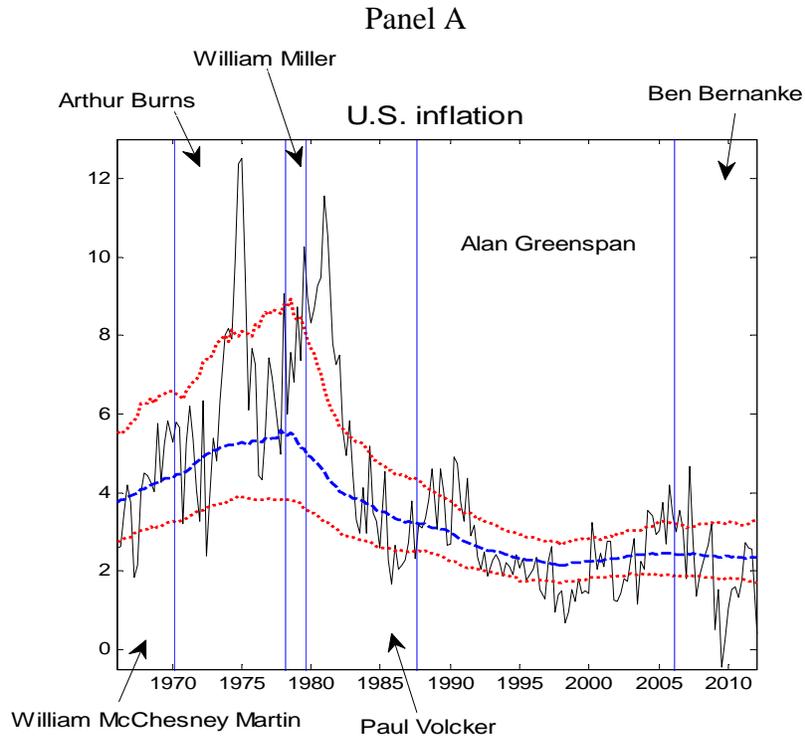


Figure 3A: Actual GDP deflator inflation rates (solid line) and estimated trend – median (dashed line) and 16<sup>th</sup> and 84<sup>th</sup> percentiles (dotted lines).

Panel A: United States over the period 1965Q4 to 2011Q4.

Panel B: United Kingdom over the period 1975Q2 to 2011Q4.